

Week 0 - examples on logarithms

Sept. 10, 2015

Example 1.

Solve the following equations

a. $9^{x^2-3x+3/2} = 1/3$

$$\begin{aligned} 9^{x^2-3x+3/2} &= \frac{1}{3} \\ \log_9(9^{x^2-3x+3/2}) &= \log_9\left(\frac{1}{3}\right) \\ x^2 - 3x + \frac{3}{2} &= \frac{\log_3(1/3)}{\log_3 9} \\ x^2 - 3x + \frac{3}{2} &= \frac{\log_3 1 - \log_3 3}{\log_3 3^2} \\ x^2 - 3x + \frac{3}{2} &= \frac{0 - 1}{2} \\ x^2 - 3x + \frac{3}{2} + \frac{1}{2} &= 0 \\ x^2 - 3x + 2 &= 0 \\ (x - 2)(x - 1) &= 0 \\ x &= 2, 1 \end{aligned}$$

b. $2^{\log_3(x+2)} = 5$

$$\begin{aligned} 2^{\log_3(x+2)} &= 5 \\ \log_2 2^{\log_3(x+2)} &= \log_2 5 \\ \log_3(x+2) &= \log_2 5 \\ 3^{\log_3(x+2)} &= 3^{\log_2 5} \\ x+2 &= 3^{\log_2 5} \\ x &= 3^{\log_2 5} - 2 \end{aligned}$$

Example 2.

In the following equation, make y the subject: $\log_y 3 = x^2 - 2x$

$$\begin{aligned}\log_y 3 &= x^2 - 2x \\ \frac{\log_3 3}{\log_3 y} &= x^2 - 2x \\ \log_3 y &= \frac{1}{x^2 - 2x} \\ y &= 3^{1/(x^2 - 2x)}\end{aligned}$$