

## Solving Systems Algebraically

By SUBSTITUTION

Ex 1

$$5x - y = 10$$

$$x^2 + x - 2y = 0$$

① Isolate the "y" in the simpler equation

$$\rightarrow 5x - \underbrace{y}_{-y} = 10$$

$$-y = -5x + 10$$

$$\underline{y} = \underline{5x - 10}$$

② Substitute what y equals into the OTHER equation

$$\rightarrow x^2 + x - 2(\underline{5x - 10}) = 0$$

$$x^2 + x - 10x + 20 = 0$$

$$x^2 - 9x + 20 = 0$$

$$(x - 4)(x - 5) = 0$$

$$\text{so } \underline{x = 4} \text{ or } \underline{x = 5}$$

$$\text{and } y = 5x - 10 \text{ so } \underline{(4, 10)} \text{ or } \underline{(5, 15)}$$

③ Simplify & solve

Check:  $5x - y = 10$

$$5(4) - (10) = 10$$

$$5(5) - 15 = 10$$

$$x^2 + x - 2y = 0$$

$$(4)^2 + 4 - 2(10) \stackrel{?}{=} 0$$

$$16 + 4 - 20 \stackrel{?}{=} 0$$

$$(5)^2 + 5 - 2(15) \stackrel{?}{=} 0$$

$$25 + 5 - 30 \stackrel{?}{=} 0$$

Questions : Section 8.2 pg 451

#3

AND: ①  $p = 3k + 1$

$$p = 6k^2 + 10k - 4$$

## Solving by Elimination:

- The goal is to ELIMINATE one of the variables by adding the two equations together.
- Start by writing one equation above the other and lining up like terms.

Ex:  $5x - y = 10$  and  $x^2 + x - 2y = 0$

$$\begin{array}{r} x^2 + x - 2y = 0 \\ -2(5x - y = 10) \\ \hline x^2 + x - 2y = 0 \\ -10x + 2y = -20 \\ \hline \end{array}$$

To eliminate the 'y's, we multiply the 2nd equation by -2

$$x^2 - 9x = -20$$

Then, solve it!

$$x^2 - 9x + 20 = 0$$

$$(x - 4)(x - 5) = 0$$

$x = 4$  or  $5$  then go back & figure out  $y$ ...

$$2\left(\frac{3}{2}x^2 - \frac{1}{2}x - \frac{1}{2}y = 1\right) \Rightarrow 3x^2 - x - y = 2$$

$$2\left(\frac{3}{2}x^2 + 2x - \frac{1}{2}y = 2\right) \Rightarrow 3x^2 + 4x - y = 4$$

$$\begin{array}{r} \textcircled{0} \qquad \qquad \textcircled{0} \\ 3x^2 - x - y = 2 \\ -3x^2 - 4x + y = -4 \\ \hline \end{array}$$

$$-5x = -2$$

$$x = \frac{2}{5} \quad \text{then go find } y \text{ \& check!!}$$

Solve using elimination:

Pg 452 #4 and #5

Use  
elim.

Use elim. or  
subst. → whichever  
you prefer.