

# IMPLICIT DIFFERENTIATION:

EXPLICIT → stated openly or directly.

IMPLICIT → implied, not stated directly.

$y = 3x + 2$  is explicit  
 $f(x) = 3x + 2$

$3x^2y^3 + 6xy^2 + 7y - 2 = 5$

There is an "implicit" relationship between  $x$  &  $y$ , but it is not defined explicitly.

$\frac{dy}{dx}$  or  $y'$

IMPLICIT  
 $\frac{d}{dx} (x^2 + y^2 = 25)$

$2x + 2y \cdot y' = 0$   
 $-2x$                        $-2x$

$y' = -\frac{2x}{2y}$

$y' = -\frac{x}{y}$

$y^2 = 25 - x^2$   
 $y = \pm\sqrt{25 - x^2}$

EXPLICIT

$y^2 = 25 - x^2$

$y = \pm\sqrt{25 - x^2}$

$y = \pm(25 - x^2)^{1/2}$

$y' = \pm \frac{1}{2} (25 - x^2)^{-1/2} (-2x)$

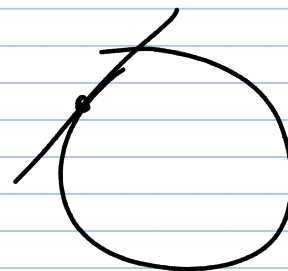
$y' = \pm \frac{x}{\sqrt{25 - x^2}}$

$\frac{-x}{\pm\sqrt{25 - x^2}}$

$y' = -\frac{x}{y}$

$y' = \frac{4}{3}$

m of  $(-4, 3)$



Ex 2  $\frac{d}{dy} (2x^5 + x^4y + y^5 = 36)$

find  $\frac{dy}{dx}$   
and the eq<sup>n</sup> of  
the tangent  
line at (1,2)

$10x^4 + x^4(1) \cdot y' + 4x^3y + 5y^4 \cdot y' = 0$

$10x^4 + x^4 \cdot y' + 4x^3y + 5y^4 \cdot y' = 0$

$x^4 + 5y^4 = -10x^4 - 4x^3y$

$y' \frac{(x^4 + 5y^4)}{(x^4 + 5y^4)} = \frac{-10x^4 - 4x^3y}{(x^4 + 5y^4)}$

$y' = \frac{-10x^4 - 4x^3y}{x^4 + 5y^4}$

$\begin{matrix} x & y \\ (1, & 2) \end{matrix}$

$= \frac{-10(1)^4 - 4(1)^3(2)}{1^4 + 5(2)^4} = \frac{-18}{81} = \frac{-2}{9}$

$y - 2 = \frac{-2}{9}(x - 1)$

$9y - 18 = -2x + 2$

$2x + 9y - 20 = 0$  ü

## Circles

$x^2 + y^2 = 1$  is a circle, centred at  $(0,0)$  with a radius of 1

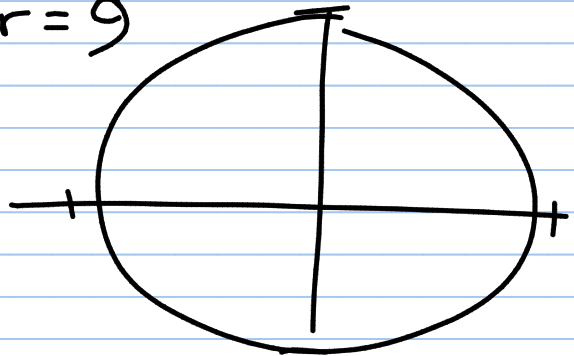
$x^2 + y^2 = 25$   $(0,0)$   $r=5$

$x^2 + y^2 = 81$   $(0,0)$   $r=9$

$(x-3)^2 + (y-2)^2 = 100$

$(3,2)$   $r=10$

$$\frac{x^2}{2} + \frac{y^2}{4} = 10$$



## 2.8 Higher Order Differentiation:

$$f(x) = 6x^5$$

$$f'(x) = 30x^4$$

$$f''(x) = 120x^3$$

$$f'''(x) = 360x^2$$

$$f^{(4)}(x)$$

$$f''(x) = \frac{d}{dx} \left( \frac{dy}{dx} \right)$$

$$= \frac{d^2 y}{dx^2}$$

$$f'''(x) = \frac{d^3 y}{dx^3}$$

$d = \dots - t$   
 $d' = v = \text{velocity.}$   
 $d'' = \text{acceleration}$   
 $d = v_0 t + \frac{1}{2} a t^2$   
 $d' = v_0 + a t$   
 $d'' = a$   
 $d''' =$

$$y = x^4 + 2x^3 - 5x^2 + 3x - 6$$

$$y' = 4x^3 + 6x^2 - 10x + 3$$

$$y'' = 12x^2 + 12x - 10$$

$$y''' = 24x + 12$$

$$y^{(4)} = 24$$

$$y^{(5)} = 0$$

Now do  
2.7 & 2.8

