

5.1 Working With Radicals Pg 279

1.

$$4\sqrt{7} = \sqrt{16} \cdot \sqrt{7} = \sqrt{112}$$
$$5\sqrt{2} = \sqrt{25} \cdot \sqrt{2} = \sqrt{50}$$
$$-11\sqrt{8} = -\sqrt{121} \cdot \sqrt{8} = -\sqrt{968}$$
$$-10\sqrt{2} = -\sqrt{100} \cdot \sqrt{2} = -\sqrt{200}$$

2.

a) $\sqrt{56} = \sqrt{4} \cdot \sqrt{14} = 2\sqrt{14}$

b) $3\sqrt{75} = 3 \cdot \sqrt{25} \cdot \sqrt{3} = 3 \cdot 5 \cdot \sqrt{3} = 15\sqrt{3}$

c) $\sqrt[3]{24} = \sqrt[3]{8} \cdot \sqrt[3]{3} = 2\sqrt[3]{3}$

d) $\sqrt{c^3d^2} = \sqrt{c^2} \cdot \sqrt{c} \cdot \sqrt{d^2} = c\sqrt{c}d$

3. a) $3\sqrt{8m^4} = 3 \cdot \sqrt{4} \cdot \sqrt{2} \cdot \sqrt{m^4} = 3 \cdot 2 \cdot \sqrt{2} \cdot m^2$
 $= 6m^2\sqrt{2}$
 $m \in \mathbb{R}$

b) $\sqrt[3]{24q^5} = \sqrt[3]{8} \cdot \sqrt[3]{3} \cdot \sqrt[3]{q^3} \cdot \sqrt[3]{q^2}$
 $= 2 \cdot \sqrt[3]{3} \cdot q \cdot \sqrt[3]{q^2}$
 $= 2q\sqrt[3]{3q^2} \quad q \in \mathbb{R}$

c) $-2\sqrt[5]{160s^5t^6} = -2\sqrt[5]{32} \cdot \sqrt[5]{5} \cdot \sqrt[5]{s^5} \cdot \sqrt[5]{t^5} \cdot \sqrt[5]{t}$
 $= -2 \cdot 2 \cdot \sqrt[5]{5} \cdot s \cdot t \cdot \sqrt[5]{t}$
 $= -4st\sqrt[5]{5t} \quad s, t \in \mathbb{R}$

$$4. a) \sqrt{3n} \sqrt{5} = \sqrt{9} \cdot \sqrt{n^2} \cdot \sqrt{5} = \sqrt{45n^2} \quad n \in \mathbb{R}$$

$$b) \sqrt[3]{-432} = \sqrt[3]{-216} \cdot \sqrt[3]{2} = -6 \sqrt[3]{2}$$

$$c) \frac{1}{2a} \sqrt[3]{7a} = \sqrt[3]{\frac{1}{8}} \cdot \sqrt[3]{\frac{1}{a^3}} \cdot \sqrt[3]{7a} = \sqrt[3]{\frac{7a}{8a^3}} = \sqrt[3]{\frac{7}{8a^2}}$$

$$a \neq 0$$

$$d) \sqrt[3]{128x^4} = \sqrt[3]{64} \cdot \sqrt[3]{2} \cdot \sqrt[3]{x^3} \cdot \sqrt[3]{x}$$

$$= 4 \sqrt[3]{2} \cdot x \cdot \sqrt[3]{x}$$

$$= 4x \sqrt[3]{2x} \quad x \in \mathbb{R}$$

$$5. a) 15\sqrt{5} \text{ and } 8\sqrt{25}$$

$$\rightarrow 8 \cdot \sqrt{25} \cdot \sqrt{5} = 8 \cdot 5 \cdot \sqrt{5} \\ = 40\sqrt{5}$$

$15\sqrt{5}$ and $40\sqrt{5}$ are like radicals

$$b) 8\sqrt{112z^8} \text{ and } 48\sqrt{7z^4}$$

$$\downarrow \\ 8 \cdot \sqrt{16 \cdot 7} \cdot \sqrt{z^8}$$

$$\downarrow \\ 48 \sqrt{7} \cdot \sqrt{z^4}$$

$$8 \cdot 4 \cdot \sqrt{7} \cdot z^4$$

$$48 \cdot z^2 \sqrt{7}$$

$$\underline{32z^4\sqrt{7}} \text{ and } \underline{48z^2\sqrt{7}}$$

Radicals are now the same
but they are NOT like terms
since there are different
powers of z

$$c) -35\sqrt[4]{w^2} \text{ and } 3\sqrt[4]{81w^{10}}$$

$$\begin{aligned} & \downarrow \\ & 3\sqrt[4]{81} \cdot \sqrt[4]{w^8} \cdot \sqrt[4]{w^2} \\ & = 3 \cdot 3 \cdot w^2 \cdot \sqrt[4]{w^2} = 9w^2\sqrt[4]{w^2} \\ & -35\sqrt[4]{w^2} \text{ and } 9w^2\sqrt[4]{w^2} \end{aligned}$$

$$d) 6\sqrt[3]{2} \text{ and } 6\sqrt[3]{54}$$

$$\begin{aligned} & \downarrow \\ & 6\sqrt[3]{27} \cdot \sqrt[3]{2} \\ & 6 \cdot 3 \cdot \sqrt[3]{2} \\ & 6\sqrt[3]{2} \text{ and } 18\sqrt[3]{2} \end{aligned}$$

$$6. a) \begin{aligned} 3\sqrt{6} &= \sqrt{9} \cdot \sqrt{6} = \sqrt{54} \quad \textcircled{1} & \text{or } 3\sqrt{6}, 7\sqrt{2}, 10 \\ 10 &= \sqrt{100} \quad \textcircled{3} \\ 7\sqrt{2} &= \sqrt{49} \cdot \sqrt{2} = \sqrt{98} \quad \textcircled{2} \end{aligned}$$

$$b) \begin{aligned} -2\sqrt{3} &= -\sqrt{12} \quad \textcircled{1} \\ -4 &= -\sqrt{16} \quad \textcircled{3} \\ -3\sqrt{2} &= -\sqrt{18} \quad \textcircled{4} \\ -2\sqrt{\frac{7}{2}} &= -\sqrt{\frac{28}{2}} = -\sqrt{14} \quad \textcircled{2} \end{aligned}$$

$$\text{so: } -2\sqrt{3}, -2\sqrt{\frac{7}{2}}, \text{ ~~-4~~, } -3\sqrt{2}$$

$$c) \begin{aligned} \sqrt[3]{21} &= \sqrt[3]{21} \quad \textcircled{1} \\ 3\sqrt[3]{2} &= \sqrt[3]{27} \cdot \sqrt[3]{2} = \sqrt[3]{54} \quad \textcircled{4} \\ 2.8 &= \sqrt[3]{21.952} \quad \textcircled{2} \\ 2\sqrt[3]{5} &= \sqrt[3]{8} \cdot \sqrt[3]{5} = \sqrt[3]{40} \quad \textcircled{3} \end{aligned}$$

$$\textcircled{3} \text{ so: } \sqrt[3]{21}, 2.8, \sqrt[3]{40}, 2\sqrt[3]{5}$$

$$8. a) -1\sqrt{5} + 9\sqrt{5} - 4\sqrt{5} = 4\sqrt{5}$$

$$b) 1.4\sqrt{2} + 9\sqrt{2} - 7 = 10.4\sqrt{2} - 7$$

$$c) 14 - 4\sqrt{11} \quad \text{or} \quad -4\sqrt{11} + 14$$

$$d) -\frac{2}{3}\sqrt{6} + 2\sqrt{10}$$

$$9. a) \begin{aligned} & 3\sqrt{75} - \sqrt{27} \\ & 3\sqrt{25 \cdot 3} - \sqrt{9 \cdot 3} \\ & 3 \cdot 5\sqrt{3} - 3\sqrt{3} \\ & 15\sqrt{3} - 3\sqrt{3} = \underline{\underline{12\sqrt{3}}} \end{aligned}$$

$$b) \begin{aligned} & 2\sqrt{18} + 9\sqrt{7} - \sqrt{63} \\ & 2\sqrt{9 \cdot 2} + 9\sqrt{7} - \sqrt{9 \cdot 7} \\ & 2 \cdot 3\sqrt{2} + 9\sqrt{7} - 3\sqrt{7} \\ & = \underline{\underline{6\sqrt{2} + 6\sqrt{7}}} \end{aligned}$$

$$c) \begin{aligned} & -8\sqrt{45} + 5.1 - \sqrt{80} + 17.4 \\ & -8\sqrt{9 \cdot 5} + 5.1 - \sqrt{16 \cdot 5} + 17.4 \\ & -8 \cdot 3\sqrt{5} - 4\sqrt{5} + 22.5 \\ & -24\sqrt{5} - 4\sqrt{5} + 22.5 \\ & = \underline{\underline{-28\sqrt{5} + 22.5}} \end{aligned}$$

$$d) \begin{aligned} & \frac{2}{3} \sqrt[3]{81} + \frac{1}{4} \sqrt[3]{375} - 4\sqrt{99} + 5\sqrt{11} \\ & \cdot \frac{2}{3} \sqrt[3]{27 \cdot 3} + \frac{1}{4} \sqrt[3]{125 \cdot 3} - 4\sqrt{9 \cdot 11} + 5\sqrt{11} \\ & \frac{2}{3} \cdot 3\sqrt{3} + \frac{1}{4} \cdot 5\sqrt{3} - 4 \cdot 3\sqrt{11} + 5\sqrt{11} \\ & 2\sqrt{3} + \frac{5}{4}\sqrt{3} - 12\sqrt{11} + 5\sqrt{11} \\ & \frac{13}{4}\sqrt{3} - 7\sqrt{11} \end{aligned}$$

$$10a) 2a\sqrt{a} + 6a\sqrt{a} \quad a \geq 0$$

$$= 8a\sqrt{a}$$

$$b) 3\sqrt{2x} + 6\sqrt{2x} - \sqrt{x}$$

$$= 9\sqrt{2x} - \sqrt{x} \quad x \geq 0$$

$$c) -4 \cdot 5\sqrt[3]{5r} + 2r\sqrt[3]{5r}$$

$$= -20\sqrt[3]{5r} + 2r\sqrt[3]{5r} \quad r \in \mathbb{R}$$

Factor out a 2: $2(-10\sqrt[3]{5r} + r\sqrt[3]{5r})$

Factor out a $2\sqrt[3]{5r}$ then:

$$-20\sqrt[3]{5r} + 2r\sqrt[3]{5r} = 2\sqrt[3]{5r}(-10 + r)$$

$$3x^2 + 6x$$

$$3x(x+2)$$

$$d) \frac{w}{5} \cdot -4 + \frac{8w}{5} - \frac{2 \cdot 5\sqrt{2w}}{5} - 4\sqrt{2w}$$

$$= -\frac{4}{5}w + \frac{8}{5}w - 6\sqrt{2w}$$

$$= \frac{4}{5}w - 6\sqrt{2w} \quad w \geq 0$$

$$15. A = \pi r^2 \quad \text{so} \quad \frac{\pi r^2}{\pi} = \frac{38\pi \text{ m}}{\pi}$$

$$\sqrt{r^2} = \sqrt{38 \text{ m}}$$

$$\underline{\underline{r = \sqrt{38 \text{ m}}}}$$

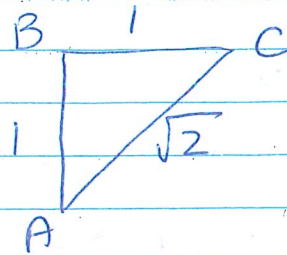
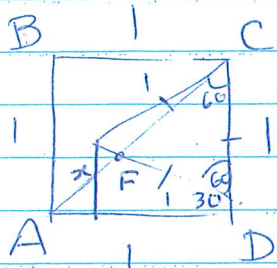
$$d = 2\sqrt{38 \text{ m}} \quad \text{b/c } 2r = d$$

Challenge

21 $\square ABCD$

Perimeter = 4 m

so each side = 1 m



(Pythagoras)

$$x\sqrt{2} =$$

$$\left(\frac{1-\sqrt{3}}{2}\right)\sqrt{2} = \frac{2\sqrt{2}-\sqrt{6}}{2}$$

$$\frac{2\sqrt{2}}{2} - \frac{2\sqrt{2}-\sqrt{6}}{2}$$