

The factor theorem:

If  $\underline{x-a}$  is a factor of  $P(x)$ , then  
 $P(a) = 0$  (the remainder is zero!)

$(x-3) \leadsto$  root:  $+3$

Ex:  $(Kx^3 + 3x + 1) \div (x+2)$  the remainder is 3.  
 Find  $\underline{K}$ .

$$P(\underline{-2}) = 3$$

$$K(-2)^3 + 3(-2) + 1 = 3$$

$$-8K - 6 + 1 = 3$$

$$\frac{-8K}{-8} = \frac{8}{-8}$$

$$K = -1$$

3.2 #8 + ...



$$P(3) = \underline{\underline{0}}$$

$$P(-7) = 0$$

$$P(1i) = \underline{\underline{3}}$$

Is  $x+2$   
 $\downarrow$   
 $-2$

Factor  $(x-3)$

$(x+7)$

$(x-11)$   $\rightarrow$  R of 3

a factor of

$\pm 1, \pm 2$

$3x^4 + 5x^3 + x(-2)$  ?

NO  $\swarrow$

$$3(-2)^4 + 5(-2)^3 + (-2) - 2 =$$

$$48 + -40 - 2 - 2 = \underline{\underline{4}}$$

$$P(x) = x^4 + 4x^3 - 7x^2 - 34x - 24$$

Possible roots:  
 $\pm 1, \pm 2, \pm 3,$   
 $\pm 4, \pm 6, \pm 8,$   
 $\pm 12, \pm 24$

$$P(-1) = 1 + -4 - 7 + 34 - 24 = 0$$

$(x+1)$

$$\begin{array}{r|rrrrr} -1 & 1 & 4 & -7 & -34 & -24 \\ & \downarrow & -1 & -3 & +10 & +24 \\ \hline & 1 & \underline{3} & -10 & -24 & \underline{0} \end{array}$$

$$1x^3 + 3x^2 - 10x - 24$$

$$P(-2) = (-2)^3 + 3(-2)^2 - 10(-2) - 24 = -8 + 12 + 20 - 24 = 0$$

$(x+2)$

$$\begin{array}{r|rrrr} -2 & 1 & 3 & -10 & -24 \\ & \downarrow & -2 & -2 & +24 \\ \hline & 1 & \underline{1} & -12 & \underline{0} \end{array}$$

$$x^2 + x - 12$$

$$(x+4)(x-3)$$

$$x^4 + 4x^3 - 7x^2 - 34x - 24 = (x+1)(x+2)(x+4)(x-3)$$

