# The Economics of Cross-Border Travel<sup>\*</sup>

Ambarish Chandra<sup>a</sup>

Keith  $\operatorname{Head}^{b,c}$ 

Mariano Tappata<sup>b</sup>

April 4, 2013

<sup>a</sup>: University of Toronto, Rotman School of Management

<sup>b</sup>: University of British Columbia, Sauder School of Business

 $^{c}$ : CEPR

#### Abstract

We model the decision to travel across an international border as a trade-off between benefits derived from buying a range of products at lower prices and the costs of travel. We estimate the model using micro-data on Canada-US travel. Price differences motivate cross-border travel; our estimates indicate that a 10% home appreciation raises the propensity to cross by 8% to 26%. The larger elasticity arises when the home currency is strong, a result predicted by the model. Distance to the border strongly inhibits crossings, with an implied cost of 87 cents/mile. Geographic differences can partially explain why American travel is less exchange-rate responsive.

<sup>\*</sup>Corresponding author: keith.head@sauder.ubc.ca. An earlier version of this paper was titled "Consumer Arbitrage Across a Porous Border." We thank participants at seminars at Cornell, Penn State, Ryerson, University of British Columbia, University of Toronto, UTDT, UdeSA, and the 2011 RMET conference for helpful comments. Suggestions by Pinelopi Goldberg, Gita Gopinath, Andy Neumeyer, Andrés Rodríguez-Clare, Gordon Hanson, and three anonymous referees proved particulary useful. This research was supported by the Social Sciences and Humanities Research Council.

# 1 Introduction

International border crossings retain a vital influence on the economy since they are the sites where governments control the movement of goods and people between nations. Most economic research on people crossing borders considers permanent migration. Far less is known about the causes and consequences of short-term movement. Nevertheless, at many borders travel flows dwarf permanent movement. For example, 50 million car trips were made across the US-Canada border in 2010, about 250 times the number of permanent migrants arriving from Canada or the US in that year.<sup>1</sup> Understanding travel patterns has important implications for taxation, infrastructure planning, securing borders, and controlling the spread of infectious diseases.

Given the magnitude and policy relevance of cross-border travel, it has attracted surprisingly little formal analysis by economists. One possible explanation is the perception that travel motivations are non-economic. Since travellers by definition return to their country of residence, this normally precludes earning income in the visited country. We must therefore look to motivations other than labor supply to explain most international travel.<sup>2</sup> This paper estimates a model in which the consumption motive drives short-term travel between Canada and the US.

After establishing stylized facts using descriptive statistics and reduced-form regressions, we develop the first model of the decision by residents of one country to cross the border and purchase a cheaper bundle of goods in the other country. Whereas models of the migration decision view potential crossers as maximizing earnings, we offer instead a model in which consumers seek to minimize expenditures.<sup>3</sup> The model combines the decision of *whether to cross* with that of *what to buy* if one crosses. Because a stronger home currency expands the set of goods that are cheaper in the foreign country, the benefits of crossing are shown to be a convex function of the real exchange rate. Estimates of the model's parameters provide robust support for this hypothesis. Evaluated at 2010 exchange rates, the crossing elasticity is 2.6, three times the elasticity observed when the currency is weak, and higher than the Blonigen and Wilson (1999) estimates for the responsiveness of US-Canada trade in goods.

The consumption motive for travel is predicated on the existence of price differences. Evidence of such differences on either side of the Canada-US border has been convincingly demonstrated by a series of papers. Engel and Rogers (1996) study of price dispersion between cities in Canada and the US reports that crossing the border is equivalent to a distance of 1,780 miles. While this estimate of the border's width has been challenged by Gorodnichenko and Tesar (2009), empirical studies consistently find price differences.<sup>4</sup> Recent work has compared disaggregated price data for

<sup>&</sup>lt;sup>1</sup>Source: Statistics Canada and Migration Policy Institute.

<sup>&</sup>lt;sup>2</sup>For the US and Canada commuters constitute only 5% of daytrips.

<sup>&</sup>lt;sup>3</sup>See Grogger and Hanson (2011) for an estimated model in which income maximization drives the decision to emigrate.

<sup>&</sup>lt;sup>4</sup>Goldberg and Knetter (1997) summarizes the earlier literature.

identical goods on both sides of the Canada-US border at stores owned by the same large retailer. Burstein and Jaimovich (2009) find substantial amounts of pricing to market. Gopinath et al. (2011) also find evidence of market segmentation, including a 24% discontinuity in grocery prices at the border. Price differences on identical products are not unique to grocery products, nor to the Canada-US border. Boivin et al. (2012) show that even online book prices differ greatly between the US and Canada, and that their prices do not respond to exchange rate movements. Goldberg and Verboven (2004) compare prices for the same car model in different European countries and report price ranges of about 35% for the majority of models in the period before the euro was introduced.

Prior studies of cross-border travel for consumption purposes have tended to examine price or tax differences across jurisdictions for specific goods, and have inferred travel from measures of sales or retail activity. Asplund et al. (2007) infer cross-border shopping for alcohol between Sweden and Denmark by observing how retail sales respond to changes in taxes and exchange rates. Manuszak and Moul (2009) examine how differences in gasoline and cigarette taxes create incentives to cross US state borders, and thereby calculate consumers' travel costs. Inferring interstate travel from variation in lottery revenues per resident, Knight and Schiff (2012) find that higher jackpots induce cross-border purchases in small, densely populated states. To our knowledge, Chiou and Muehlegger (2008) is the only paper that uses direct data on travel across borders to estimate responses to price differences (caused by cigarette taxes). Moving beyond studies of individual goods, Campbell and Lapham (2004) and Baggs et al. (2010) find that exchange rate changes affect the employment and exit of retail firms located near the US-Canada border. Their results are consistent with cross-border shopping behavior, but they do not estimate travel responses directly.

Our paper proceeds in three steps. First, we use reduced form regressions in Section 2 to establish that travelers respond strongly to the economic incentives created by fluctuations in the exchange rate. This finding corroborates results from reduced form estimations conducted by Di Matteo and Di Matteo (1993, 1996) and Ferris (2000, 2010). We also find that travel by Canadian residents has a higher elasticity with respect to the exchange rate than US travel. Moreover, for residents of both countries, these elasticities increases in absolute value as the home currency strengthens. To make sense of these findings and to allow investigations of counterfactuals, our second step is to develop a model of the decision to cross based on the premise that travellers seek bargains on the other side of the border. The model presented in Section 3 naturally generates the prediction that the elasticity of crossings rises in absolute value as the home currency strengthens. The third step is to use a new dataset with information on the residence of cross-border travellers to estimate the parameters of the model. The strong travel responses we estimate imply the markets are not perfectly segmented. However, travel costs prevent the arbitraging away of all price differences. Our estimated coefficients imply that the median crosser requires savings of 87 cents per mile traveled. As a consequence, shopping motivated travel is concentrated among the population living close to the border. Indeed, the median day tripper in Canada lives 18 miles from the border whereas the median Canadian lives 81 miles away.

The model also permits counterfactual experiments. We show that an exogenous doubling of border wait times would lower crossing frequencies by 50–60%. We estimate that travel has fallen by 32% since September 11, 2001, compared with the otherwise expected level of travel given the realized values of the exchange rate, gaso-line prices, income, and population. The model provides a natural way to calculate the average crosser's welfare gains in response to changes in the explanatory variables. We find that a 10% appreciation from current rates would yield average crosser gains of 2.1% whereas the consequences of 9/11 have lowered these gains by 3.4%. We also show that differences in the geographic distribution of residents partially explain the difference in the Canadian and US travel elasticities.

# 2 Stylized facts of border crossings

In this section we describe our cross-border travel data and establish the main relationships between exchange rates and travel between Canada and the US.

### 2.1 Data

Statistics Canada provides data on cross-border travel using information collected by the Canadian Border Services Agency (CBSA).<sup>5</sup> These data consist of counts of all vehicles entering Canada at all land crossings with the United States. US residents encounter the CBSA on their outbound journey and Canadian residents on their return journey.

We use these data on vehicle counts for the 7 Canadian provinces that share a land border with the United States: British Columbia, Alberta, Saskatchewan, Manitoba, Ontario, Quebec and New Brunswick. We use monthly data on passenger vehicles for the calendar years 1972–2010. The counts are broken down by travelers' country of residence, which is determined by whether the vehicle has US or Canadian license plates, and by the length of the cross-border trip. We analyze same-day and overnight (here defined as trips spanning two or more days) trips separately.

We obtained monthly average data on the spot market exchange rate between the US and Canadian currencies. Using data on monthly CPIs for both countries we construct the Real Exchange Rate (RER) for each month.<sup>6</sup> It is defined with US prices in the numerator such that RER increases correspond to Canadian dollar depreciations. We fixed the absolute level of the RER using relative price levels from OECD data.

<sup>&</sup>lt;sup>5</sup>See Cansim Table 427-0002.

<sup>&</sup>lt;sup>6</sup>The consumer price indexes include sales taxes. Data sources and other details are provided in the online appendix.

Figure 1 displays key temporal patterns in the data.<sup>7</sup> Figure 1(a) shows the ratio of monthly same-day trips by residents of the two countries from 1972 through 2010. The solid blue line shows the real exchange rate. The dashed blue line shows the monthly nominal exchange rates, expressed in the figure as an index of the July 1993 level (1.29 CAD per USD), when the RER was approximately one (that is, prices of the consumer bundle expressed in a common currency were approximately equal). Because both countries have mainly had similar inflation rates, the primary source of real exchange rate variation is nominal variation.<sup>8</sup> US trips rise relative to Canadian trips when the US has relatively high price levels. Since the 1980s the relationship between relative travel and the exchange rate has become very strong.





Travel is highly seasonal for residents of both countries. Figure 1(b) shows average travel over the 38-year period for each calendar month. Cross-border travel rises with average temperatures, peaking in July and August, for all groups. One interpretation, to which we return when we estimate the model, is that cold weather raises travel costs. Figure 1(b) also serves to show relative magnitudes of the different travel categories. Over the 1972–2010 period Canadian residents averaged about 50% more daytrips across the border than US residents. Overnight trips have similar monthly means for North- and South-bound travelers.

We employ the CBSA data in the reduced form regressions that follow. However, for the model we estimate in Section 4, we require information on the geographic distribution of crossers and the distance they travel to and from the border. This

<sup>&</sup>lt;sup>7</sup>Table 1 in the online appendix to this paper presents summary statistics for these data.

<sup>&</sup>lt;sup>8</sup>More precisely, log first differences of the nominal exchange rate explain 94% of the variation in log first differences of the real exchange rate over the period 1972–2010. In levels the  $R^2$  is 0.89.

information is not available in the CBSA data, so we use a second source of data on cross-border travel: the International Travel Survey (ITS), which is also made available by Statistics Canada. This survey is based on questionnaires filled out by travelers returning to Canada. It collects information on the nature and purpose of the trip, the dates on which travelers exited and entered Canada, the Census Division in which the travelers reside, and the ports used to cross to the US. We retain data on Canadian residents returning from the United States by car between 1990 and 2013.<sup>9</sup> The ITS data contains 63000 observations, each corresponding to a Canadian census division in a given month. Summary statistics of the ITS data are reported in Table 2 in the online appendix.

The ITS data indicate that a majority of cross-border trips are made for pleasure or personal reasons, which include shopping trips. These sorts of trips are potentially the most likely to respond to exchange rates. Trips for the purpose of business or driving to work, which are likely to be less sensitive to the exchange rate, account for under 10% of responses.<sup>10</sup> This suggests that the exchange rate potentially plays an important role in the decision to cross the border. We now attempt to quantify the relationship between exchange rates and cross-border travel.

#### 2.2 The Exchange Rate Elasticity of Cross-Border Travel

Our first regression exercise is to determine the elasticity of cross-border trips with respect to the real exchange rate. Our goal is establish simple data relationships to motivate the development of a model in the subsequent section of the paper. We therefore work with a minimal specification. Denoting the number of cars that cross the border by n, and the real exchange rate by e, our specification is:

$$\ln n_{it} = \text{Month}_t + \text{Province}_i + \eta_1 \ln e_t + \eta_2 \text{post}911_t + \eta_3 t + \eta_4 t^2 + \varepsilon_{it}, \qquad (1)$$

where i denotes a province and t denotes time (in months since January 1972). The month effects account for the strong seasonality in travel. We add province fixedeffects, as well as an indicator variable for the period following September 11, 2001 when border security was increased. Finally, we add a linear and quadratic trend to capture secular effects such as population changes. We estimate this equation separately for residents of each country. Therefore, for Canada, this regression models the number of cars returning from the US in a given province and month. For the US, it represents the cars that enter the corresponding Canadian province.

Implicit in the estimation of equation 1 is the assumption that causation runs only from the real exchange rate to crossing decisions. This assumption is defensible because demand for foreign currency created by US and Canadian cross-border shoppers

<sup>&</sup>lt;sup>9</sup>We do not use information on US residents since the only information on their place of residence within the US is the state in which they live. This level of aggregation is too coarse to provide meaningful information on their distance to the border.

<sup>&</sup>lt;sup>10</sup>In Table 3 in the online appendix, we tabulate the commonly stated motives for crossing the border, using ITS data on visitors and returning residents to Canada.

is unlikely to be large enough to move the global foreign exchange markets. To gain some perspective on relative magnitudes, Canadians spent \$4.2bn in the US while Americans spent \$1.8b in Canada during the first quarter of 2010.<sup>11</sup> This represents a mere 0.04% of the foreign exchange turnover involving the Canadian Dollar.<sup>12</sup>

Length of stay:	Daytrip		Over	night	Daytrip		Overnight	
Residence:	US	CA	US	CA	US	CA	US	CA
$\ln e$	$1.24^{a}$	$-1.62^{a}$	$0.47^{a}$	$-1.78^{a}$	$0.93^{a}$	$-1.71^{a}$	0.32	$-2.08^{a}$
(CAD/USD)	(0.17)	(0.24)	(0.17)	(0.17)	(0.28)	(0.28)	(0.23)	(0.21)
$\ln e \times [e > 1.09]$					$0.90^{b}$	$0.54^{c}$	$0.83^{a}$	$0.65^{b}$
(strong USD)					(0.37)	(0.33)	(0.31)	(0.29)
$\ln e \times [e < 0.90]$					$-0.87^{b}$	$-0.87^{a}$	$-1.25^{a}$	-0.31
(strong CAD)					(0.34)	(0.24)	(0.32)	(0.22)
$R^2$	0.98	0.98	0.96	0.97	0.98	0.98	0.97	0.97

Table 1: Regression of log crossings, 1972–2010.

New ey-West standard errors in parentheses are robust to serial correlation out to 60 months. An observation is a province-year-month. Regressions include month and province fixed-effects, a post 9/11 indicator, and trend variables. N=3276. <sup>c</sup> p < 0.1, <sup>b</sup> p < 0.05, <sup>a</sup> p < 0.01

The results of estimating this equation are presented in Table 1. We treat each province in a calendar month as a separate observation. Since monthly crossing data are serially correlated, we use Newey-West standard errors. The results in the first four columns indicate that travelers respond to the exchange rate, as represented in the negative elasticity of Canadian residents and the positive elasticity of US residents with respect to the real exchange rate. In addition, the elasticities of Canadian residents are bigger than those of US residents, for same-day and overnight trips.

In columns 5–8 we investigate whether the crossing elasticity with respect to exchange rates varies with the level of the exchange rate. We find significant interactions between the log of the RER and indicators for the highest and lowest quartiles of the RER over the 38-year period. In particular, the coefficient for the period when the US dollar was strong is generally positive, for residents of both countries. This has the effect of increasing the positive elasticity of US residents, and decreasing the negative elasticity of Canadian residents. In other words, US residents become more responsive to the exchange rate in periods when the US dollar is strong, while Canadian residents become less responsive. We observe the opposite pattern during periods when the US dollar is in its lowest quartile.<sup>13</sup>

<sup>&</sup>lt;sup>11</sup>This includes expenditures by air travelers. Source: International Travel Account Receipts and Payments (http://statcan.gc.ca/daily-quotidien/100827/dq100827-eng.pdf)

<sup>&</sup>lt;sup>12</sup>Source: Authors' calculations from the BIS Central Bank Survey of Foreign Exchange and Derivatives Market Activity, 2010 (http://www.bis.org/publ/rpfxf10t.htm)

<sup>&</sup>lt;sup>13</sup>Tables 4, 5 and 6 in the online appendix show that these results are robust to using country-level data, taking first differences of Equation 1, and adding economic indicators as regressors.

This section has uncovered four stylized facts of cross-border travel that should be features of a quantitative model of crossing decisions. First, while there is always two-way movement across the border, there are large within- and between-year fluctuations. Second, there is a robust relationship between exchange rates and travel: the stronger the currency in the country of residence, the more trips. Third, elasticities are asymmetric: In absolute value Canadian residents have higher percentage responses to changes in the exchange rate. Fourth, exchange rate elasticities are larger when the home currency is stronger.

## 3 Model of the crossing decision

Potential cross-border shoppers must decide whether it is worth incurring travel costs to obtain shopping benefits. The benefits are modeled using a continuum of goods structure similar to Dornbusch, Fischer, and Samuelson (1977). To focus on the crossing decision, we omit the supply-side of that model. We show that the model generates a convex relationship between the savings obtained from cross-border shopping and real exchange rates that rationalizes the findings of the previous section.

Consumers purchase a continuum of goods on the unit interval. Good z has price P(z) in the home country and a price  $P^*(z)$  in the foreign country, with both prices expressed in local currency units. Let E represent the nominal exchange rate defined in home currency unit per foreign currency unit. Define  $\bar{P}$  and  $\bar{P}^*$  as the domestic and foreign consumer price indexes. The real exchange rate, which indicates the relative price of the foreign consumption bundle expressed in a common currency is given by  $e = E\bar{P}^*/\bar{P}$ . Lastly, we define  $\delta(z)$  as the relative price deviation of good z:

$$\delta(z) = \frac{P(z)/P}{P^*(z)/\bar{P}^*}.$$
(2)

We order goods such that  $\delta'(z) > 0$  and assume that relative price deviations are invariant to the real exchange rate, that is  $\partial \delta(z)/\partial e = 0$ .<sup>14</sup>

The borderline good for which prices are equal after converting currency, is denoted  $\tilde{z}$  and defined implicitly as  $P(\tilde{z}) = EP^*(\tilde{z})$ . Substituting this relationship and the definition of the real exchange rate back into equation (2), it follows that  $\delta(\tilde{z}) = e$ . Goods  $z < \tilde{z}$  are cheaper at home and the remaining goods are cheaper abroad. Inverting  $\delta(z)$ , we find  $\tilde{z} = \delta^{-1}(e)$ , with  $\partial \tilde{z}/\partial e = 1/\delta'(\tilde{z}) > 0$ . Thus, a real appreciation of the foreign currency contracts the range of goods that are cheaper in the foreign country.

Figure 2 illustrates the model using data from Porter (2009). The author reports prices for 19 goods available on both sides of the border. Calculating  $\delta(z)$  as the ratio of the Canadian price (in CAD) to the US price (in USD), all divided by the relative price level (1.2, obtained from the OECD) we plot it against z. The study was

<sup>&</sup>lt;sup>14</sup>The online appendix shows that this result is implied by the DFS supply side assumptions.



Figure 2: Exchange rates and relative prices: 19 products

conducted when the exchange rate was 1.09 CAD/USD, leading to a real exchange rate of e = 0.91. With a Canadian dollar at this strength, 15 out of 19 goods were less expensive in the US after converting prices to a common currency. The figure shows that seven goods—from cars to MacBooks—would switch to being cheaper in Canada if the USD appreciated by 10% to e = 1.

To take advantage of lower prices in foreign retail stores, the consumer engages in cross-border shopping. Thus wholesalers can trade goods across borders but, due to pricing-to-market by home retailers, consumers can only obtain the foreign price by travelling to the foreign retail store.<sup>15</sup> Individuals decide whether to stay at home or cross by comparing the indirect utility associated with each option. Consumers have Cobb-Douglas utility with expenditure share parameters b(z). Stayers, who spend their whole income, W, in the home country have indirect utility given by

$$v_S = \ln W - \int_0^1 b(z) \ln P(z) dz.$$

Crossers buy goods  $\tilde{z} \leq z \leq 1$  in the foreign country but make the rest of their purchases at home. Travel costs take the "iceberg" form:  $1 - 1/\tau$  is the fraction of income that "melts away" in the trip across the border.<sup>16</sup> Neglecting any home government taxes on the goods travelers bring back, the price paid for foreign goods is  $EP^*(z)$  in domestic currency.<sup>17</sup> Finally we assume a non-pecuniary benefit (or cost,

<sup>&</sup>lt;sup>15</sup>An implicit assumption is that the proportion of cross-border shoppers is not large enough to have a material effect on pricing decisions by firms on either side of the border.

<sup>&</sup>lt;sup>16</sup>In the empirical work, travel costs are a function of distance to the border, gas prices, and time costs.

<sup>&</sup>lt;sup>17</sup>Adding a tax would just be a scalar multiplying the real exchange rate.

if negative) of travel given by  $\zeta$ . The indirect utility of crossers is therefore given by

$$v_X = \ln W/\tau - \int_0^{\tilde{z}} b(z) \ln P(z) dz - \int_{\tilde{z}}^1 b(z) \ln EP^*(z) dz + \zeta.$$

The model should not be taken literally since cars cannot physically accommodate all the products that are cheaper in the foreign country. The important idea is that the indirect utility of a cross-border trip depends on the prices of the goods that a consumer would actually choose to buy in the foreign country.

The net benefits of crossing is obtained by subtracting  $v_S$  from  $v_X$ , yielding

$$v_X - v_S = B - \ln \tau + \zeta, \tag{3}$$

where  $B \equiv \int_{\tilde{z}}^{1} b(z) [\ln P(z) - \ln EP^{*}(z)] dz$ , the gross benefit of crossing, is the savings from buying goods in the foreign country instead of domestically. For any interior value of  $\tilde{z}$ , B is positive since  $P(z) > EP^{*}(z)$  for all  $z > \tilde{z}$ .

Using the notation of DFS we also define  $\vartheta(\tilde{z}) = \int_0^{\tilde{z}} b(z) dz$  as the share of expenditures on goods for which the home country is the low-price supplier. Inserting the definitions of e,  $\delta(z)$  and  $\vartheta$  into B, we express the benefits of crossing as a function of the log real exchange rate:

$$B(\ln e) = -(1 - \vartheta(\tilde{z}))\ln e + \int_{\tilde{z}}^{1} b(z)\ln\delta(z)dz.$$
(4)

The first term shows that, holding  $\tilde{z}$  constant, a stronger foreign currency lowers the benefit of crossing. The second term can be thought of as the correlation between budget shares and price deviations for the set of goods  $z > \tilde{z}$ . It says that the benefits of crossing are higher if consumers happen to particularly like the goods that are relatively expensive at home.

Noting that  $\vartheta'(\tilde{z}) = b(\tilde{z})$ , the derivative of (4) with respect to  $\ln e$ , while holding  $\delta(z)$  constant,<sup>18</sup> can be expressed as

$$B' = -(1 - \vartheta(\tilde{z})) + b(\tilde{z})(\ln \delta(\tilde{z}) - \ln e)\frac{\partial \tilde{z}}{\partial \ln e} = -(1 - \vartheta(\tilde{z})) < 0.$$
(5)

The impact of the exchange rate on the benefits of crossing depends on the share of goods that are cheaper abroad:  $1 - \vartheta(\tilde{z})$ . Foreign appreciation (rising *e*) contracts that share, leading to a benefit function that is convex in the real exchange rate:

$$B'' \equiv \frac{\partial^2 B}{\partial \ln e^2} = b\left(\tilde{z}\right) \frac{\partial \tilde{z}}{\partial \ln e} = b\left(\tilde{z}\right) \frac{\delta(\tilde{z})}{\delta'(\tilde{z})} > 0.$$
(6)

The convexity of the  $B(\ln e)$  function arises under general functional form assumptions for preferences, b(z), and relative price deviations  $\delta(z)$ .

<sup>&</sup>lt;sup>18</sup>We assume that changes in  $\ln e$  are generated by changes in the nominal exchange rate E or by proportional shocks to all prices such as ad valorem taxes or factor price increases.

Individual heterogeneity enters the net benefits of crossings in two ways. First, the non-pecuniary benefits of crossing,  $\zeta$ , assumed to be distributed with a CDF denoted  $F(\zeta)$ . Second, we add community c subscripts to the determinants of travel costs to reflect differences in distance to the border and wages ( time costs). Within each community c there is a marginal individual who is indifferent between crossing and staying. This  $\zeta_c^*$  is defined by setting  $v_X = v_S$ , yielding  $\zeta_c^* = -B(\ln e) + \ln \tau_c$ . Thus, residents of distant communities (high  $\tau_c$ ) require a higher idiosyncratic shock to justify crossing the border. With a continuum of individuals, the fraction of crossers, denoted  $x_c$ , will be equal to the probability that a potential crosser has  $v_X > v_S$ :

$$x_c = \mathbb{P}(\zeta_c^* < \zeta) = F(B(\ln e) - \ln \tau_c).$$
(7)

The model's predicted exchange rate and travel costs elasticities depend on the curvature of the CDF, but both are unambiguously negative:

$$\frac{\partial \ln x_c}{\partial \ln e} = \frac{F'}{F}B' = -\frac{F'}{F}[1 - \vartheta(\tilde{z})] < 0, \qquad \qquad \frac{\partial \ln x_c}{\partial \ln \tau_c} = -\frac{F'}{F} < 0. \tag{8}$$

The regressions in section 2 showed that the exchange rate elasticity of travel diminishes in periods when the foreign currency is strong. Differentiating the first equation in (8) yields

$$\frac{\partial^2 \ln x_c}{\partial \ln e^2} = \frac{[FF'' - (F')^2]}{F^2} (B')^2 + \frac{F'}{F} B''.$$

This expression reveals that once heterogeneity is added into the model, the positive second derivative of the individual benefit function (B'') shown in (6) will not translate into a positive second derivative for aggregate log crossings if the term in brackets is sufficiently negative. However, convexity in the benefit function is almost a necessary condition for convexity in log crossings. This is because the term in square brackets is negative for most distributions of individual heterogeneity.<sup>19</sup>

A second reduced-form finding we would like to reconcile with the model is that crossers from Canadian provinces into US states exhibit higher exchange rate elasticities than residents of the US states on the other side of the border. In the context of our model, this can happen if Canadians spend a higher share of their income on goods that are cheaper in the US than vice-versa. As shown in the online appendix, the model also predicts elasticities to differ in response to different population distributions, a hypothesis we confirm after estimating the model.

# 4 Estimation of the model

In order to estimate the crossing fraction equation shown in (7), we need to parameterize the crossing benefit and cost functions (B and  $\ln \tau_c$  in equation (3)) as well as

 $<sup>^{19}</sup>F'/F$  is globally decreasing for uniform, normal, logit, gumbel, and power-law distributions.

specify the distribution of individual heterogeneity  $(F(\zeta))$ . We use a quadratic form for  $B(\ln e)$  in our empirical specification since it is the simplest way to capture and test for convexity:

$$B(\ln e) = \beta_0 + \beta_1 \ln e + \beta_2 [\ln e]^2.$$
(9)

The model predicts  $B' = \beta_1 + 2\beta_2 \ln e < 0$  for the observed range of e and  $B'' = 2\beta_2 > 0$ . Equation (9) can be justified as a second-order approximation of a general B or, as shown in the online appendix, as the exact form implied by two additional assumptions on prices and budget shares.

The next step is to parameterize  $\tau_c$  in terms of its underlying observable determinants. The cost of the cross-border trip consists of the sum of the opportunity cost of driving time and fuel costs. Letting parameters  $\psi$  equal speed (kilometer per hour),  $\phi$  equal fuel efficiency (kilometers per liter), and H equal the endowment of hours, the total crossing cost is  $D_c[W_c/(\psi H) + P(g)_c/\phi]$ , where  $P(g)_c$  is the price of gasoline (per liter) and  $D_c$  is driving distance (in kilometers). Expressing travel costs in iceberg form (the ratio of initial income to income after deducting travel costs) yields

$$\tau_c = \left[1 - D_c \left(\frac{1}{\psi H} + \frac{P_c(g)}{\phi W_c}\right)\right]^{-1}.$$
(10)

We see that the strict iceberg assumption of a constant fraction of income lost from travel is only met in the limit as the gas price to income ratio goes to zero. To facilitate estimation, we use a linear-in-logs approximation of equation 10:

$$\ln \tau_c = \gamma_0 + \gamma_1 \ln D_c + \gamma_2 \ln \left[ P(g)_c / W_c \right]. \tag{11}$$

The  $\gamma_0$  parameter shifts travel costs at all distances. One such shifter would be border formality compliance costs.<sup>20</sup> The  $\gamma_1$  parameter represents the elasticity of travel costs with respect to distance.

We assume that  $\zeta$  in equation 7 follows a normal distribution, with expectation  $\mu$ and variance  $\sigma^2$ . Adding time subscripts and substituting the functions  $F(\zeta)$ , B and  $\ln \tau$  into equation 7, we can express the crossing fraction as

$$x_{ct} = \Phi[\theta_0 + \theta_1 \ln e_t + \theta_2 (\ln e_t)^2 + \theta_3 \ln D_c + \theta_4 \ln (P(g)_{ct}/W_{ct})],$$
(12)

where the coefficients are the model parameters are scaled by the standard deviation of individual heterogeneity (e.g.  $\theta_1 = \beta_1/\sigma$ ). The parameter  $\theta_0 = (\beta_0 - \gamma_0 + \mu)/\sigma$ , is allowed to vary across months and provinces, reflecting seasonal and geographic influences on the average non-pecuniary benefits ( $\mu$ ) and costs ( $\gamma_0$ ) of travel.

When taking equation 12 to the data we should replace  $x_{ct}$  with its conditional expectation:  $\mathbb{E}[x_{ct} \mid e_t, D_c, P(g)_{ct}, W_{ct}]$ . Deviations between observed crossing fractions and those predicted by the model arise from at least two sources. First, the

 $<sup>^{20}\</sup>mathrm{Our}$  specification includes a dummy for periods after September, 2001 to capture changes in border impediments.

continuum assumption is only an approximation, so the actual crossing share would only be equal to the crossing probability in expectation. Second, the data that we use for estimation are the ITS data, described in Section 2.1, which are based on a survey given out to a subset of the actual population of crossers.

When estimating this equation, we need to recognize that the dependent variable is a fractional response bounded between 0 and 1. As Table 2 in the online appendix shows, in many census-divisions the number of cars crossing the border is zero. It is important to employ an estimation method that (a) incorporates zeros into the estimation and (b) does not yield out-of-bounds predictions. We therefore estimate the expected crossings equation as fractional probit model. This method yields consistent estimates of the model parameters so long as the conditional expectation  $\mathbb{E}[x_{ct} | \cdot]$  is correctly specified. Had we assumed that F is logistic, it would have been possible to take the log of the odds, x/(1-x), and obtain a right hand side that is linear in the parameters and therefore estimable using OLS. We show the results for this approach in the robustness section but do not adopt it as the main method for two reasons. First, the log odds is undefined at the limit values and thus can induce selection bias by dropping observations with zero crossings. Second, it does not estimate the conditional expectation of  $x_{ct}$  consistently.<sup>21</sup>

The dependent variable is the crossing fraction,  $x_{ct}$ , which is defined as the number of car crossings,  $n_{ct}$ , from Census Division (CD) c in month t, divided by the number of potential crossings,  $N_{ct}$ . Potential crossings are approximated as the population of the census division (Pop), multiplied by the number of cars per capita (CPC) in the province multiplied by the number of days in the month. Thus, the crossing fraction is given by

$$x_{ct} = \frac{n_{ct}}{N_{ct}} \approx \frac{\hat{n}_{ct}}{\operatorname{Pop}_{ct} \times \operatorname{CPC}_c \times 30}.$$
(13)

We estimate  $\hat{n}_{ct}$  using data from the International Travel Survey (ITS), which was described in Section 2.1. The online appendix shows the sources for the variables in equation 13 and details how we construct  $\hat{n}_{ct}$  by weighting the ITS responses using the port-level counts of all crossers, so as to make the sample representative at the monthly level as well as representative at each port of entry.

We measure  $D_c$ , the distance from census division c to the border, in two ways described in the online appendix. Our preferred form is the population-weighted median of the driving distances of all the subdivisions within a given CD.<sup>22</sup> In robustness checks we also measure  $D_c$  as the median driving time to these ports, and as the average of driving distances to the five most-used ports. Gas prices, P(g), are obtained for the largest city in each province. Median household income, our proxy for  $W_c$ , is

<sup>&</sup>lt;sup>21</sup>Papke and Wooldridge (1996) explain this defect and other advantages of the fractional probit method.

<sup>&</sup>lt;sup>22</sup>Figure D.1 in the online appendix contains a map of a few CDs in south-eastern Ontario, showing the subdivisions within each CD. The map shows that driving distances are needed (rather than great-circle distances) to take into account the Great Lakes.

available at the CD-level from the Canadian census every five years.<sup>23</sup>

### 4.1 Baseline Estimation

We estimate the model parameters in equation 12 separately for travelers making same-day and overnight (stays of two or more days) trips. Travelers whose main reason for crossing the border is to shop are much more likely to make same-day trips, and is these travelers whose behavior is represented in the model. By contrast, those making overnight trips may have purposes other than just shopping for goods to bring home: vacations, recreation spanning multiple days, visiting acquaintances etc. For these travelers, the single-good model sketched in the online appendix may be more appropriate. On a related note, same-day and overnight travelers may respond differently to gasoline prices and other travel cost shocks, as we discuss below.

The results using the fractional probit method of estimation are presented in Table 2. The first three columns use daytrips to construct the dependent variable, while the next three use overnight trips. All estimated specifications include (unreported) month dummies to allow shocks to the mean of the  $\zeta(i)$  distribution reflecting the seasonal pattern shown in Figure 1(b). Standard errors are clustered at the census division (c) level to allow for arbitrary serial correlation within divisions.<sup>24</sup> The initial specification, shown in columns 1 and 4, assumes that travel costs are constant across time and depend only on the distance of the traveler's origin to the border. Columns 2 and 5 estimate the influence of gas prices and incomes. We do not report the specification imposing equal and opposite coefficients on  $\ln P(q)$  and  $\ln W$  because we found that the same day travel data strongly reject this constraint. Our preferred specification, shown in columns 3 and 6, adds fixed effects (FE) for each province and a dummy for travel after September, 2001. The province FEs capture differences in  $B(\ln e)$  that result from unmeasured cross-state differences in product prices.<sup>25</sup> We focus on the third specification since adding province fixed-effects improves the fit of the model considerably.

The coefficients on the exchange rate variables indicate that a higher value of the real exchange rate (implying a weaker CAD) reduces the probability of cross-border trips. The coefficient on the squared term is positive for daytrips, implying that travelers' responsiveness to the real exchange rate decreases as its level rises. This accords with the predictions of our model and is also consistent with the reduced form results of Table 1. Residents making daytrips are more likely to expand the bundle of goods that they purchase in the US when the exchange rate becomes more favorable.

<sup>&</sup>lt;sup>23</sup>Data details and sources are provided in the online appendix.

 $<sup>^{24}</sup>$ Ideally we would use two-way clustering of standard errors, to account for each census division in month t having the same real exchange rate. While this is not currently feasible using fractional probit, it is feasible in the log-odds estimation which is another advantage of using that method as a robustness check.

 $<sup>^{25}</sup>$ They can also account for differences in the mean idiosyncratic shocks due to different population densities on the US side of the border which affect the likelihood of visiting friends and relatives.

Length of stay:		Daytrip			Overnigh	nt
$\theta_0$ : constant	-0.23	$9.80^{a}$	$4.42^{a}$	$-2.68^{a}$	$-4.59^{a}$	$-5.20^{a}$
	(0.31)	(2.94)	(1.52)	(0.07)	(0.57)	(0.99)
$\theta_1$ : $\ln e_t$ [RER]	$-0.44^{a}$	$-0.77^{a}$	$-0.65^{a}$	$-0.61^{a}$	$-0.92^{a}$	$-0.75^{a}$
	(0.10)	(0.14)	(0.13)	(0.12)	(0.13)	(0.12)
$\theta_2$ : $(\ln e_t)^2$	0.39	$1.24^{a}$	$0.82^{b}$	-0.09	0.27	-0.17
	(0.34)	(0.33)	(0.33)	(0.30)	(0.28)	(0.24)
$\theta_3$ : $\ln D_c$ [distance]	$-0.58^{a}$	$-0.58^{a}$	$-0.52^{a}$	$-0.14^{a}$	$-0.14^{a}$	$-0.12^{a}$
	(0.06)	(0.06)	(0.04)	(0.01)	(0.01)	(0.01)
$\ln P(g)_{ct}$ [gas price]		$-0.35^{a}$	-0.07		$-0.56^{a}$	$-0.13^{a}$
		(0.09)	(0.05)		(0.04)	(0.02)
$\ln W_{ct}$ [income]		$-0.80^{a}$	$-0.42^{a}$		$0.40^{a}$	$0.29^{a}$
		(0.27)	(0.14)		(0.06)	(0.09)
Post-911			$-0.14^{a}$			$-0.14^{a}$
			(0.03)			(0.03)
$R^2$	0.24	0.29	0.53	0.05	0.07	0.08

Table 2: Fractional Probit estimation of crossing fractions  $(x_{ct})$ 

Standard errors clustered by census-division. Regressions include month FEs. Columns 3 and 6 include province FEs.  $^c$  p<0.1,  $^b$  p<0.05,  $^a$  p<0.01. N = 63000

We do not observe the same behavior by overnight travelers: the coefficients on  $[\ln e_t]^2$  are small and statistically insignificant in columns 4–6. This may be because overnight travelers are more likely to purchase a standard bundle of goods in the US (hotel stays, vacations, restaurant meals etc.) without adjusting the scope of the bundle in accordance with relative prices. This still implies a positive elasticity of overnight travel with respect to the home currency, but does not imply that the elasticity changes with the RER. In other words, day trips are consistent with the multi-product shopping motive, whereas overnight trips instead appear to better fit with a single-good model such as the one in the online appendix.

Examining expenditure data provides additional support for this hypothesis. The International Travel Survey asks returning residents about their purchases made outside the country. These figures are subject to travelers' accurate recollection and truthful reporting of these amounts, and are therefore noisy and potentially biased. Nevertheless, our examination of reported expenditures shows that same-day travelers have a positive elasticity of spending with respect to the home currency, while overnight travelers exhibit no effect of the exchange rate on their spending.<sup>26</sup>

Turning to travel costs, the results show that driving distance creates a strong disincentive to cross the border. This is especially the case for daytrips; distance is

<sup>&</sup>lt;sup>26</sup>See Table 8 in the online appendix for these results.

a weaker disincentive for those planning trips of a longer duration. High gas prices lower overnight travel significantly as expected for variables that increase travel costs. The coefficient on log gas prices in column 6 is about the same as the distance coefficient. The negative effect on day-trippers is smaller and imprecisely measured. Its confidence intervals include the coefficient for overnight trips (-0.13), as well as zero. The effect of gas prices in Canada may be harder to discern for same-day travellers because the majority live less than 18 miles from the border and can fill up at US prices at gas stations south of the border.

Income effects are strongly negative for day-trippers. This runs counter to what would be expected if income mattered just because it affects the fuel cost to income ratio in  $\tau$ . Our model assumes a constant marginal utility of income across all individuals. One interpretation of the results is that richer households are less motivated by the savings to be had from cross-border shopping. For overnight trips income effects are positive. In column 6 the regression does not reject the restriction of equal and opposite effects for gas prices and incomes that is predicted by the transport cost function shown in equation 10.

The downward shift in travel to the US following September, 2011 has a distance equivalent given by  $\exp(0.14/0.52) - 1 = 0.31$ . Thus, the extra costs of crossing the border in the years since 9/11 correspond to a 31% increase in distance. Alternatively, using a counterfactual calculation of the kind described in Section 4.4, we find a total reduction of 32% in travel attributable to 9/11. Remarkably, given the many differences in method, Ferris (2010) reports a 29% annual reduction.

Figure 3 illustrates the magnitudes of the estimated effects graphing predicted crossing shares as functions of our key explanatory variables. This is important since the estimated coefficients are scaled by the unobserved  $\sigma$  parameter. Moreover, the effects of the RER and distance have to pass through the nonlinear  $\Phi()$  function to determine the predicted crossing share. We show the relationship between the crossing fraction and the real exchange rate for specific distances from the border in panel (a). It is based on the specification in column 3 of Table 2 (adjusting using the coefficients on the Ontario, post 9/11, and April dummy variables). Each curve corresponds to a census division in Southern Ontario. The curves show that the convexity in the *B* function carries over to the log crossing function. Thus, the elasticity of crossing is larger in absolute value when the home currency is strong. Furthermore, the elasticity of crossing implied by the model is larger at greater distances from the border. We can see this in the figure as the curve for Toronto is steeper (which corresponds to greater elasticity since both axes are drawn on a log scale) than that for Niagara.

The main determinant of travel costs is distance to the border. Figure 3(b) shows the steep decline of crossing fractions associated with increased driving distances. The curve graphs the average of the predicted shares (in percent) that would cross from each Ontario census division during the sample period (1990–2010). The circles show actual crossing fractions averaged over the same period. The model fits the data well, further supporting the validity of the linear-in-logs approximation of the travel



Figure 3: Crossing declines with foreign appreciation and distance to the border

cost function. Divisions further from the border than Toronto (about 90 miles) have predicted and actual crossing rates below 0.1%. This means that on any given day there is a less than 1 in 1000 chance for a car to be driven across the US border on a daytrip. By contrast, communities closer than Niagara (15 miles) have crossing rates that are more than an order of magnitude higher.

#### 4.2 Robustness to specification changes and falsification tests

In Table 3 we present results from a number of different specifications and variable definitions. We use the set of controls corresponding to columns 3 and 6 of Table 2. The first two columns of Table 3 present results using the log of the odds of travel  $(x_{ct}/(1 - x_{ct}))$  as the dependent variable and estimating with OLS. The remaining columns return to the fractional probit model, but use different measures of the costs of travel. In columns 3 and 4 we use the driving *time* to the border from each Census Division, instead of the driving distance, using information from Google on differences in average driving speeds relevant for different subdivisions. We add 26 minutes to the driving time to account (very roughly) for border wait times.<sup>27</sup> In columns 5 and 6 we use our secondary measure of distance (detailed in the online appendix). Relative to the primary measure used in Table 2, it has the advantage of taking into account not just the nearest port but the five ports that residents of the CD use most

 $<sup>^{27}</sup>$ There is no source for nation-wide wait time data. 26 minutes is the median wait for travelers entering the US during 7 AM – 12 PM at the two largest ports in British Columbia, using daily data from 2006 to 2010. Source: Whatcom Council of Governments.

frequently. It has the disadvantage of using the geographic center of the CD as the origin point, which exaggerate distances severely for some large Divisions.

Method:	Log Oc	lds (OLS)		Fraction	al Probit	
Stay:	Daytrip	Overnight	Daytrip	Overnight	Daytrip	Overnight
$\theta_0$ : constant	$25.40^{a}$	-2.28	$5.07^{a}$	$-5.22^{a}$	$10.33^{a}$	$-4.61^{a}$
	(3.14)	(1.87)	(1.82)	(1.01)	(2.47)	(1.08)
$\theta_1$ : $\ln e_t$	$-1.55^{a}$	$-2.00^{a}$	$-0.65^{a}$	$-0.75^{a}$	$-0.65^{a}$	$-0.75^{a}$
	(0.25)	(0.15)	(0.13)	(0.12)	(0.13)	(0.12)
$\theta_2$ : $(\ln e_t)^2$	$3.73^{a}$	0.20	$0.93^{a}$	-0.15	$1.03^{a}$	-0.16
	(0.73)	(0.63)	(0.33)	(0.24)	(0.32)	(0.24)
$\theta_3$ : ln dist. or time	$-1.14^{a}$	$-0.28^{a}$	$-0.89^{a}$	$-0.19^{a}$	$-0.56^{a}$	$-0.14^{a}$
	(0.07)	(0.04)	(0.06)	(0.02)	(0.05)	(0.02)
$\ln P(g)_{ct}$	-0.15	$-0.42^{a}$	-0.05	$-0.13^{a}$	-0.03	$-0.13^{a}$
	(0.13)	(0.08)	(0.05)	(0.02)	(0.05)	(0.02)
$\ln W_{ct}$	$-2.41^{a}$	-0.19	$-0.64^{a}$	$0.26^{a}$	$-0.94^{a}$	$0.25^{b}$
	(0.30)	(0.17)	(0.18)	(0.10)	(0.24)	(0.10)
Post-911	$-0.25^{a}$	$-0.18^{a}$	$-0.13^{a}$	$-0.14^{a}$	$-0.12^{a}$	$-0.14^{a}$
	(0.06)	(0.04)	(0.03)	(0.03)	(0.03)	(0.03)
Observations	24232	33771	63000	63000	63000	63000
$R^2$	0.51	0.28	0.57	0.08	0.51	0.08

Table 3: Alternative specifications of regression and travel costs

Standard errors clustered by census-division except cols. (1)–(2) where SEs also clustered by month-year. Regressions include month, province FEs.  $^{c}$  p<0.1,  $^{b}$  p<0.05,  $^{a}$  p<0.01. Driving time in cols. (3)–(4); port-use weighted average distances in cols. (5)–(6).

Our chief results on exchange rate and distance effects hold in all specifications. The positive second-order effect for exchange rates continues to hold for daytrips and is insignificant for overnight trips. Travel costs, whether measured in terms of distance or time, have a negative and strongly significant effect on the probability of crossing the border; much more so for daytrips than overnight ones.

There are a number of other robustness checks that we conducted, the results of which are contained in Table 7 in the online appendix. We included a quadratic term for distance but it was not statistically significant, nor did it contribute significantly to the fit of the model. We also dropped observations where the drive times were extraordinarily long (more than 12 hours in one specification and more than 3 in another). We examined whether commuters—residents of Canada who work in the United States—impact our results, since these travelers cross the border daily regardless of the exchange rate, and therefore are not the type of travelers that the model considers.<sup>28</sup> Dropping the census divisions where commuters made up 10% or more of travelers leads to very similar results.

While all regressions in Table 2 control for the average seasonal pattern in travel using month dummies, we also estimated regressions (Table 9 in the online appendix) that directly include monthly weather data, as measured for the principal city in each province). In the absence of month effects, higher mean temperatures raise crossing propensities. When month effects are included, weather does not have a significant effect on day trips, indicating that the regular pattern of the seasons explains sameday travel behaviour but idiosyncratic weather deviations do not. Overnight trips do respond to unusually bad weather, with sharp dips in months with high snowfall. Overall, our findings with regard to gas prices and weather are consistent with our results regarding exchange rates, and show that travelers respond appropriately to changes in the costs or benefits of travel.

The real exchange rate and distance terms enter the crossing equation 12 additively. This suggests a simple falsification test. If the model is correctly specified, there should be no significant interaction between exchange rates and distance. When we add such an interaction term to the estimating equation, it is not statistically significant and it does not improve the  $R^2$  relative to the equation implied by our model, as shown in Column 3 of Table 7 in the online appendix.

A second way to validate the model draws upon the interpretation of the seasonality captured in the month effects. If seasons matter because they increase marginal travel costs, then they should have a greater impact on residents living further from the border. Furthermore they should have no interaction with the shopping benefits of crossing captured in the real exchange rate. To test these predictions, we interact the month dummies with  $\ln D_c$  and, separately, with  $\ln e_t$ . We find strong distancemonth interactions for same-day travel: the marginal impact of distance falls from -0.55 in January to -0.48 in July. On the other hand the elasticity of travel with respect to the RER does not have any significant seasonal pattern.<sup>29</sup> These results suggest a seasonal pattern to travel costs and add support for the model's implication of independence between shopping benefits and travel costs.

#### 4.3 Implied travel cost estimates

One very useful way to evaluate our coefficients is to determine what they imply about travelers' willingness to trade off savings from cross-border shopping versus travel costs. Re-expressing the net benefits of crossing,  $v_X - v_S$  in equation (3), using the parametric forms for  $B(\ln e)$  and  $\ln \tau(D)$  and setting  $\zeta = 0$  we obtain

$$v_X - v_S = \beta_0 + \beta_1 \ln e + \beta_2 [\ln e]^2 - \gamma_0 - \gamma_1 \ln(D) - \gamma_2 \ln(P(g_c)/W_c).$$

 $<sup>^{28}</sup>$ Although commuters constitute under 6% of travelers, they make up a disproportionate share in certain census divisions, such as Essex (35% commuters), just across the border from Detroit.

<sup>&</sup>lt;sup>29</sup>The p-value on the restriction that all month-RER interactions are zero is 0.7.

Totally differentiating by e and D and rearranging yields

$$\frac{de/e}{dD/D} = \frac{\gamma_1}{\beta_1 + 2\beta_2 \ln e}$$

We do not observe  $\beta_1$ ,  $\beta_2$ , or  $\gamma_1$  but we do estimate  $\theta_1 = \beta_1/\sigma$ ,  $\theta_2 = \beta_2/\sigma$ , and  $\theta_3 = -\gamma_1/\sigma$ . Plugging in these estimates, canceling out the  $\sigma$ , we obtain (de/e)/(dD/D) as a function of the estimated parameters and the level of the real exchange rate. This calculation tells us the percent change in the real exchange rate required to compensate someone for a percentage increase in the distance or duration of the cross-border trip.

To obtain the change in expenditure, X, that would be required as compensation for the trip we note that expenditure in CAD is given by e times expenditure in USD. Holding USD-denominated expenditure constant, we have dX/X = de/e. We thereby arrive at the following formula for the travel cost:

$$\frac{dX}{dD} = \frac{-\hat{\theta}_3}{\hat{\theta}_1 + 2\hat{\theta}_2 \ln e} \left[\frac{X}{D}\right].$$

At the 2010 average real exchange rate of e = 0.8846, the first factor is given by -0.611 for distance (using  $\hat{\theta}$  from column (3) of Table 2) and -1.02 for time (based on column (3) of Table 3). The second factor shown in brackets, X/D, is less straightforward to determine. We use the car-weighted median distance (or duration) of a round trip for daytrippers for D. This works out to 36 miles or 1.8 hours (including a 26 minute border wait in each direction). For X we use 51 USD, the 2010 median expenditure in the ITS of daytrippers who spent a positive amount.

Plugging in these values, we obtain a travel cost of US \$0.87 per mile or \$29.69 per hour. These figures are in line with the \$0.89 per mile reimbursement rate for government travel within Ontario,<sup>30</sup> and 2010 Canadian median hourly wages of US \$23.34 per hour.<sup>31</sup> Using means instead of medians for D (56 miles) and X (\$152) leads to travel cost estimates of \$1.66/mile and \$68.34/hour. These travel cost estimates are on the high end of the range reported in the literature on shopping within national markets.<sup>32</sup>

The normality assumption for individual heterogeneity can be replaced with assumptions of logistic or Gumbel distributions. While each distributional assumption

<sup>&</sup>lt;sup>30</sup>See http://www.njc-cnm.gc.ca/directive/travel-voyage/s-td-dv-a2-eng.php. All CAD figures in this section were converted to USD using the 2010 average exchange rate of 1.03 CAD/USD.

<sup>&</sup>lt;sup>31</sup>See CANSIM Table 2820070.

<sup>&</sup>lt;sup>32</sup>Chiou and Muehlegger (2008) estimate that consumers would be willing to travel to a location 2.7 miles further away to save \$1 on cigarettes. This equates to a travel cost of 18.5 cents per mile. Manuszak and Moul (2009) estimate a marginal cost of around 50 cents per mile for consumers of gasoline in the Chicago area. Thomadsen (2005) estimates a travel cost of around \$1.50 per mile for consumers choosing fast food restaurants in Palo Alto.

leads to different estimated coefficients, their relative values change very little. As shown Table 10 in the online appendix, the evaluation of  $-\hat{\theta}_3/(\hat{\theta}_1 + 2\hat{\theta}_2 \ln e)$  in 2010 ranges from -0.60 to -0.62, with the normal distribution in the middle. The monetary travel costs differ by only a few cents per mile, demonstrating robustness to specific distributional assumptions.

#### 4.4 Quantification: Crossing elasticities and crosser gains

In this section we consider three counterfactual exercises: (i) a 10% appreciation of the Canadian dollar in any given year, (ii) a doubling of wait times at the border, and (iii) a re-play of history without the post-9/11 depression of travel. The first experiment is particularly useful because the fractional probit coefficients, like those in a binary probit, are not directly usable. The implied aggregate travel elasticities vary with the exchange rate and also depend on the geographic distribution of distances and incomes. Elasticities must therefore be obtained numerically as the aggregation of the predicted impacts in each census division-month combination.

	RER	-10%	Wait -	+100%
Year:	2002	2010	2002	2010
Canada	8.02	25.67	-57.08	-54.60
New Brunswick	6.33	19.92	-52.29	-49.10
Quebec	10.00	32.12	-55.77	-54.04
Ontario	7.94	25.47	-60.37	-57.33
Toronto $(140 \text{ km})$	10.78	34.35	-44.74	-42.84
Hamilton $(75 \text{ km})$	9.79	31.30	-53.72	-52.32
Niagara $(24 \text{ km})$	8.08	25.21	-64.16	-62.53
Manitoba	9.76	31.35	-53.42	-51.78
Saskatchewan	10.47	34.02	-53.31	-51.48
Alberta	11.41	37.81	-50.75	-49.23
British Columbia	8.31	25.88	-55.38	-53.48

Table 4: Counterfactual effects on same-day travel probabilities

Columns 1 and 2 of Table 4 show the impact, in two different years, on the number of cross-border trips from a 10% decrease in e. This is equivalent to a strengthening of the Canadian Dollar. These estimates were derived by calculating, for each month in the corresponding year, the number of car trips from each Census Division had the RER in that month been 10% lower than its actual value. These counterfactual values were then aggregated across all census-divisions in the province and compared to the predicted values using the specification of Column 3 in Table 2. The years that we analyze are 2002 and 2010, when the Canadian Dollar was at its weakest (e = 1.30) and strongest (e = 0.88), respectively, against the US Dollar, in the last 50 years. Table 4 reveals differences in the implied exchange rate elasticities across locations and time. Comparing the three Ontario census divisions, elasticities are larger for communities located further from the border. It appears that the elasticities are also larger in provinces where most of the population is far from the border. As Figure D.2 in the online appendix shows, Alberta, Saskatchewan and Manitoba (provinces with high elasticities) have relatively few inhabitants located at or very close to the border. This finding is consistent with our discussion at the end of section 3 and in the online appendix. At a given point in time, an appreciation of the RER shifts up the benefits of crossing for all census-divisions and therefore for all provinces, leading to proportional increases in the elasticities from 2002 to 2010. The elasticities rise due to the convex relationship between the crossing benefits and the log RER.

The implied crossing elasticities can be compared to those obtained in the trade literature to gain perspective on the responsiveness of consumers to changes in relative prices. When the Canadian dollar is at its weakest (2002), the Canada-wide elasticity of 0.80 (first row of Table 4) is almost the same as the average elasticity of 0.81 of the Blonigen and Wilson (1999) estimate for Canada-US trade in goods. At the strongest levels of the RER, elasticities for travel are three times as large as those observed for goods. One reason why travel could be more elastic is that travelers can alter their border crossing decision immediately as relative prices change, whereas traders have to make various up-front investments in marketing, distribution, and logistics.

Columns 3 and 4 of Table 4 show the effect of increasing wait times at the border. We use the specification from Column 3 of Table 3, which had assumed a wait time of 26 minutes at the border. In our counterfactual experiment we double this to 52 minutes.<sup>33</sup> This naturally decreases the likelihood of cross-border trips by Canadians. However, now there are significant differences across provinces, and almost no variation over time. The smallest effects of the increased wait times are in the provinces of Alberta and New Brunswick, which do not have large cities close to the border. Since the wait time is incurred by all travelers, those driving longer distances pay a proportionately lower cost. By contrast, our model predicts a very large decrease in trips for a given increase in wait times for a province such as Ontario with a large population very close to the border.<sup>34</sup> The predicted impacts of delay do not vary much over time since the effect of travel costs is independent of the value of the RER in the net benefits function.

The structural approach has the additional advantage that the impact of changes can be expressed in terms of percent changes in surplus accruing to the average traveler. For a community with mass  $N_c$  of potential monthly crossers, aggregate

<sup>&</sup>lt;sup>33</sup>Note that this increase in wait times needs to occur for exogenous reasons such as reduced staffing at the border or an increase in the time taken to process each vehicle.

<sup>&</sup>lt;sup>34</sup>The online appendix contains a figure displaying the different geographical distributions of population across Canadian provinces.

surplus is the integral over individuals for whom  $\zeta > \zeta_c^*$ :

$$G_c = N_c \int_{\zeta_c^*}^{\infty} [B - \ln \tau_c + \zeta] dF(\zeta) = \underbrace{(B - \ln \tau_c + \mathbb{E}[\zeta \mid \zeta > -B + \ln \tau_c])}_{\text{Average crosser's gain}} \underbrace{F[B - \ln \tau_c]N_c}_{\text{Number of crossers}}.$$
(14)

To a first approximation, the percentage change in crosser welfare brought about by a change in the determinants of  $B - \ln \tau_c$  will be given by the sum of the percentage changes in the number of crossers,  $n_c$ , and the average gain each crosser expects to obtain,  $G_c/n_c$ . We therefore quantify these components separately. The difference between their sum and the total welfare effect is negligible in the experiments we conduct.

With  $\zeta$  distributed  $\mathcal{N}(\mu, \sigma^2)$ , we can compute the average crosser's gain as

$$G_c/n_c = (B - \ln \tau_c) + \mu + \sigma \frac{\phi[(\mu + B - \ln \tau_c)/\sigma]}{\Phi[(\mu + B - \ln \tau_c)/\sigma]} = \sigma \left( \mathbf{Z}\hat{\boldsymbol{\theta}}_c + \frac{\phi[\mathbf{Z}\hat{\boldsymbol{\theta}}_c]}{\Phi[\mathbf{Z}\hat{\boldsymbol{\theta}}_c]} \right), \quad (15)$$

where  $\mathbf{Z}_c$  is the vector of explanatory variables and  $\boldsymbol{\theta}$  is the coefficient vector. The second equality comes from  $(B - \ln \tau_c + \mu)/\sigma = \mathbf{Z}\hat{\boldsymbol{\theta}}_c$  (the prediction index obtained from the fractional probit regressions). Without being able to identify  $\sigma$  in equation (15), levels of  $G_c/n_c$  cannot be determined, but we can determine the percentage change resulting from any contemplated change in the  $\mathbf{Z}_c$  vector.<sup>35</sup> To quantify the aggregate effect of policy changes, it is necessary to aggregate over the effects at each census division, multiplying by  $N_c$  to give greater weight to larger divisions.

The model indicates that the home appreciation gives rise to aggregate gains of 28.20% in 2010. Most of this, 25.67%, comes from increased propensity to cross. Welfare changes for the average crosser contribute 2.22%.<sup>36</sup> The gains to the average crosser are approximately three times as high when the appreciation starts from an already strong Canadian dollar.<sup>37</sup> The biggest percentage gains to the average crosser are obtained in census divisions close to the border, with Niagara crossers gaining 2.6% from the 10% home appreciation. Increasing delays would lower average crosser gains by 4.6% in 2010 in Canada. Larger losses would occur at communities along the border where the wait constitutes a higher share of total trip length. In Niagara, for example, doubling wait times would lower average crosser gains by 9.7%.

Our final counterfactual is to "turn off" the estimated 9/11 effect. As we reported earlier, the post-9/11 period had a 32% reduction in same-day crossings relative to what the model would have predicted based on the evolution of the real exchange rate, gas prices and incomes. The average crosser incurs a 3.4% reduction in welfare.

 $<sup>^{35}</sup>$ This means that we cannot quantify the monthly welfare gains for community c relative to staying at home. All policy change exercises capture relative gains and can be applied to the daily or monthly as well as individual or collective welfare gains.

 $<sup>^{36}</sup>$ The remainder, 0.31%, is attributable to the weighted product of the changes.

<sup>&</sup>lt;sup>37</sup>As mentioned in Section 3, the benefits from crossing could be limited by car size constraints that prevent the crosser from taking full advantage of lower prices.



Figure 4: Population and Distance to the Border

### 4.5 Reconciliation with reduced-form estimates

We now return to a key result obtained in the stylized facts section: the elasticity of crossings with respect to the RER is 25% lower for Americans than for Canadians in the first two columns of Table 1. An asymmetry when the Canadian dollar is strong is a prediction that follows from equation (5) since low e would reduce  $\tilde{z}$ , raising (in absolute value) the Canadian elasticity while lowering the US one. However, the quartile specifications show that the asymmetry is found even when the RER is close to one. Here we investigate whether differences in population distributions may be partially responsible for the observed lower crossing elasticities of US residents.

We do not have data on the geographic distribution of US crossers. However, we can use our estimates to simulate cross-border travel by Canadian residents in the event that their geographic distribution resembled that of the US population most likely to make cross-border shopping trips. For this exercise, we use US population and driving distances at the census tract level. We impose a cutoff distance of US census tracts to the border of 200 km, in order for the set of included census tracts to generally resemble the Canadian census divisions that are likely to have same-day crossers; this distance bound contains about 97.5% of Canadian same-day crossers. For each US census tract we compute the predicted crossing probability, corresponding to estimating equation 12. We then conduct a counterfactual exercise similar to Section 4.4 by increasing the exchange rate by 10% in order to calculate elasticities.

Figure 4 shows the differences between the US and Canada in terms of population density and distance to the border.<sup>38</sup> Panel (a) shows that a higher proportion

<sup>&</sup>lt;sup>38</sup>The figures were constructed by calculating the driving distance from each census tract to the closest land border. Details are provided in the online appendix.

of Canadians live near the border relative to the United States. Panel (b) shows the accumulated population as we move farther from the border. The figure shows that the northern US (within about 200 kms of the border) is generally less densely populated than a similar distance cutoff in Canada.<sup>39</sup> These different distributions and population densities can affect crossing elasticities as explained in the online appendix.

The comparison of Canadian and (simulated) US elasticities is shown in Table 5. We calculate these elasticities for 2002 and 2010, in order to correspond to Table 4, as well as for 2005, which had a value of the RER close to 1. We present elasticities corresponding to each of the three specifications from Table 2. Note that the elasticities for Canada in 2002 and 2010 using the column 3 specification are the same as those reported in Table 4. The elasticities for the US use the distribution of population across US census tracts, but applied to Canadian data on incomes and gas prices, and using the coefficients estimated on the Canadian population in Table 2. Even though the column 3 specification is preferred for the structural estimation, it is not necessarily the best specification to use for this exercise. This is because using either province fixed-effects or province level income and gas prices, which are included in the specifications of Columns 2 and 3, requires assigning US census tracts to Canadian provinces in a somewhat arbitrary fashion.<sup>40</sup>

Table 3	$2002 \ (e = 1.3)$		2005 (e =	= 1.01)	$2010 \ (e = 0.88)$		
Specification	Canada	US	Canada	US	Canada	US	
Column 1	7.11	6.08	12.05	10.22	14.80	12.44	
Column 2	6.46	5.65	23.82	20.55	34.23	29.13	
Column 3	8.02	7.30	19.25	17.36	25.67	22.95	

Table 5: Counterfactual travel elasticities, with simulated US data

Canadian elasticities calculated as in Table 4. US elasticities simulated using Census tract populations, with estimated coefficients from Table 2.

The results of Table 5 suggest that changing the distribution of population in Canada to more closely reflect that of the northern US would lower the elasticity of crossings with respect to the RER. In each year, and given any of the three specifications of Table 2, the elasticity using US population data is lower than using Canadian data. In the most conservative estimate—that of Column 3—the simulated elasticities are about 10% lower using the US population distribution. In Table 1, (levels specification) Americans have 25% lower elasticities. In other words, using the US population distribution explains 40% of the difference in elasticities between Canadian and Americans. There are a variety of potential explanations for the remainder

<sup>&</sup>lt;sup>39</sup>The exception is the region within about 70 kms of the border, containing the large US cities of Buffalo and Detroit but no similar sized Canadian cities.

<sup>&</sup>lt;sup>40</sup>We assigned each US census tract to the Canadian province which is across the border from the closest port to that census tract.

of the difference, but they lie outside our model. The US side of the border might have a greater density of retail networks or offer greater variety of goods than what is available on the Canadian side of the border. In addition, the Canadian media seems to accord more attention to the level of the currency, which may prime Canadians to travel in response to favourable shifts.

# 5 Conclusion

On average, each person living within a three hour drive of the Canada-US border makes more than one cross-border car trip per year.<sup>41</sup> In this paper we develop and estimate a model of cross-border travel. In line with the shopping motive in our model, US-Canada border crossings are heavily influenced by exchange rate changes. Furthermore, the elasticity of same-day crossings with respect to the exchange rate increases with the strength of the domestic currency, as predicted by expansion of the extensive margin of purchases. Consistent with the literature documenting pricing-to-market across borders, two forces prevent prices from fully converging in the two countries. First, consumers face large marginal travel costs. Our estimates range between \$30 and \$68 per travel hour (or \$0.87 and \$1.66 per mile). Second, individuals are heterogeneous. While the majority of Canadian crossers live less than 18 miles from the border, the majority of Canadians reside more than 81 miles away. We use our estimates to show that asymmetries in the geographical distribution of the population in the two countries can partially explain the differences in the sensitivity of US and Canadian travelers to the exchange rate.

# References

- Asplund, M., R. Friberg, and F. Wilander (2007, February). Demand and distance: Evidence on cross-border shopping. *Journal of Public Economics* 91(1-2), 141–157.
- Baggs, J., E. Beaulieu, L. Fung, and B. Lapham (2010). Exchange rate movements and firm dynamics in Canadian retail industries. Working Paper.
- Blonigen, B. A. and W. W. Wilson (1999). Explaining Armington: What determines substitutability between home and foreign goods? Canadian Journal of Economics 32(1), 1–21.
- Boivin, J., R. Clark, and N. Vincent (2012). Virtual borders: Online nominal rigidities and international market segmentation. *Journal of International Economics* 86(2), 327–336.

<sup>&</sup>lt;sup>41</sup>22 million Canadians and 24 million Americans reside in this region.

- Burstein, A. and N. Jaimovich (2009). Understanding movements in aggregate and product-level real-exchange rates. Working Paper.
- Campbell, J. R. and B. Lapham (2004, September). Real exchange rate fluctuations and the dynamics of retail trade industries on the U.S.-Canada border. American Economic Review 94(4), 1194–1206.
- Chiou, L. and E. Muehlegger (2008). Crossing the line: Direct estimation of crossborder cigarette sales and the effect on tax revenues. The B.E. Journal of Economic Analysis & Policy (Contributions) 8(48), 1935–1682.
- Di Matteo, L. and R. Di Matteo (1993). The determinants of expenditures by Ccanadian visitors to the United States. *Journal of Travel Research* 31(4), 34–42.
- Di Matteo, L. and R. Di Matteo (1996). An analysis of Canadian cross-border travel. Annals of Tourism Research 23(1), 103–122.
- Dornbusch, R., S. Fischer, and P. A. Samuelson (1977, December). Comparative advantage, trade, and payments in a Ricardian model with a continuum of goods. *American Economic Review* 67(5), 823–39.
- Engel, C. and J. H. Rogers (1996, December). How wide is the border? American Economic Review 8(5), 1112–25.
- Ferris, J. S. (2000). The determinants of cross border shopping: Implications for tax revenues and institutional change. *National Tax Journal* 53(4), 801–824.
- Ferris, J. S. (2010). Quantifying non-tariff trade barriers: What difference did 9/11 make to Canadian cross-border shopping? *Canadian Public Policy* 36(4), 487–501.
- Goldberg, P. K. and M. M. Knetter (1997, September). Goods prices and exchange rates: What have we learned? *Journal of Economic Literature* 35(3), 1243–1272.
- Goldberg, P. K. and F. Verboven (2004). Cross-country price dispersion in the euro era: a case study of the European car market. *Economic Policy* 19(40), 483–521.
- Gopinath, G., P.-O. Gourinchas, C.-T. Hsieh, and N. Li (2011). International prices, costs and mark-up differences. *American Economic Review* 101(6), 2450–86.
- Gorodnichenko, Y. and L. L. Tesar (2009, January). Border effect or country effect? Seattle may not be so far from Vancouver after all. American Economic Journal: Macroeconomics 1(1), 219–41.
- Grogger, J. and G. H. Hanson (2011). Income maximization and the selection and sorting of international migrants. *Journal of Development Economics* 95(1), 42–57.

- Knight, B. G. and N. Schiff (2012, November). Spatial competition and cross-border shopping: Evidence from state lotteries. *American Economic Journal: Economic Policy* 4(4), 199–229.
- Manuszak, M. D. and C. C. Moul (2009). How far for a buck? Tax differences and the location of retail gasoline activity in Southeast Chicagoland. The Review of Economics and Statistics 91(4), 744–765.
- Papke, L. E. and J. M. Wooldridge (1996). Econometric methods for fractional response variables with an application to 401 (k) plan participation rates. *Journal* of Applied Econometrics 11(6), 619–632.
- Porter, D. (2009). Looney's leap: Mind the (price) gap. BMO Capital Markets Special Report.
- Thomadsen, R. (2005). The effect of ownership structure on prices in geographically differentiated industries. *RAND Journal of Economics* 36(4), 908–929.

# Appendices

## A Theoretical derivations

#### Supply-side determination of price deviations

The Dornbusch, Fischer, and Samuelson (1977) model implies prices (in local currency) are given by P(z) = a(z)W and  $P^*(z) = a^*(z)W^*$ . In DFS the a(z) and  $a^*(z)$  are unit labour requirements and product markets are perfectly competitive. For our purposes, the a(z) could be the product of the cost parameter and a constant good-specific markup (such as would occur in the Dixit-Stiglitz monopolistic competition model).

Utility is  $\ln U = \int_0^1 b(z) \ln C(z) dz$ , where C(z) denotes consumption of good z. With Cobb-Douglas preferences the natural definition of the price indexes are  $\bar{P} = \exp(\int_0^1 b(z) \ln P(z) dz)$  and  $\bar{P}^* = \exp(\int_0^1 b^*(z) \ln P^*(z) dz)$ . The ratio of the domestic to foreign price index is given by  $\bar{P}/\bar{P}^* = W/(W^*\kappa)$ , where

$$\kappa \equiv \exp\left(\int_0^1 [b^*(z)\ln a^*(z) - b(z)\ln a(z)]dz\right)$$

is a constant if budget shares and relative productivities across goods do not change over time. Relative price deviations are determined entirely in terms of exogenous parameters:  $\delta(z) = \kappa a(z)/a^*(z)$ . Hence under the DFS supply side assumptions,  $\delta(z)$ is not influenced by the exchange rate.

#### Derivation of quadratic benefits function

The quadratic is the exact solution under the assumptions of uniform budgeting and exponential relative price deviations, that is b(z) = 1 and  $\delta(z) = \exp[\lambda(z-1/2)]$ . The exponential deviations assumption is not as arbitrary as it might seem. Since z spans the unit interval and  $\delta(z)$  is sorted in increasing order, the  $\delta(z)$  function is actually the inverse of the the cumulative distribution function (CDF) of relative nominal prices. Hence an exponential form implies that the CDF of relative prices is linearly related to the log of  $\delta(z)$ . Strictly positive variables are often distributed log-normally in practice and this distribution has the feature that for most of the data except the tails, there is a close-to-linear relationship between the CDF and the log of the variable. Under these assumptions, the solution for the borderline good is linear in the log real exchange rate ( $\tilde{z} = \frac{1}{2} + \frac{1}{\lambda} \ln e$ ) and parameters of equation (9) have structural interpretations, with  $\beta_0 = \lambda/8$ ,  $\beta_1 = -1/2 < 0$ , and  $\beta_2 = 1/(2\lambda) > 0$ .

#### Single-good model

Suppose instead of there being a continuum of goods which are available on both sides of the border there is only a single product that potential travellers are deciding where to buy. Maintaining Cobb-Douglas, consumers spend a fixed share b of their

income on this product  $(1 - b \text{ goes to items such as rent and taxes that are only purchased in the country of residence). This could be an all-inclusive holiday at a ski resort, for example. Let local currency prices be <math>P$  and  $P^*$ . Let  $F(\zeta)$  be the CDF of the difference in perceived quality of this good between the foreign and domestic version and, as before,  $\tau_c$  is the iceberg travel cost. The indifferent potential crosser has  $\zeta_c^* = b \ln P - b \ln(EP^*) - \ln \tau_c$ . Assuming relative prices of this product are proportional to the ratio of CPIs  $(P/P^* = a\bar{P}/\bar{P}^*)$ , the fraction who cross is

$$x_c = \mathbb{P}(\zeta > \zeta_c^*) = F(b \ln a - b \ln e - \ln \tau_c).$$

This model predicts a coefficient of zero for  $[\ln e]^2$ . Moreover, since F'/F is decreasing in its argument for the distributions of F() used in fractional models (logit, probit, gumbel), the elasticity of crossings with respect to crossings will tend to *diminish* in absolute value with the strength of the home exchange rate, the opposite of our finding in section 2.

#### Geographic aggregation

To think about why a province (or country) might have a higher elasticity, we need to aggregate multiple communities c, of size  $N_c$  into a single region R of size  $N_R$ . The crossing rate of the aggregate is  $x_R = \sum_{c \in R} \frac{N_c}{N_R} x_c$ . The elasticity of crossings of this region with respect to e is given by

$$\frac{\partial \ln x_R}{\partial \ln e} = \sum_{c \in R} \frac{N_c}{N_R} \frac{x_c}{x_R} \frac{\partial \ln x_c}{\partial \ln e} = -\frac{[1 - \vartheta(\tilde{z})]}{x_R} \sum_{c \in R} \frac{N_c}{N_R} F'.$$
(16)

Inspection of equation (16) suggests various ways in which crossing elasticities can differ between regions. One way US elasticities could be smaller is if  $\vartheta(\tilde{z})$ , the expenditure share of goods that are cheaper at home, were sufficiently lower in Canada than its counterpart for the US. In the model this would occur if b(z) and  $b^*(z)$  are positively correlated with  $\delta(z)$ , that is if both countries tend to spend high shares of their incomes on goods that are relatively expensive in Canada.

Equation (16) also reveals that differences in regional elasticities can arise from differences in the geographic distribution of the potential crossers in each region. If cities in one region all have higher  $\tau_c$ ,  $x_R$  decreases and the absolute value of the crossing elasticity in equation (16) becomes larger. There is a secondary impact of higher  $\tau_c$  via changes in F'. The elasticity is only certain to rise (in absolute value) if F'' < 0 for all communities c. The analysis is further complicated when taking into account difference in the weights of potential crossers,  $N_c/N_R$ . In general, the relationship between geography and the regional exchange rate crossing elasticity must be addressed numerically.

# **B** Data construction

### **B.1** Crossing fractions

Each observation in the ITS data is a questionnaire filled out by a Canadian resident returning to Canada from a trip to the US. This includes people who enter by car, bus, train, air, foot, boat etc. A maximum of one questionnaire is given to each traveling party. We keep only those observations where the traveling party exited and reentered Canada by car. We also restrict the sample to people who reside in one of the 7 provinces that share a land border with the United States: New Brunswick, Quebec, Ontario, Manitoba, Saskatchewan, Alberta and British Columbia. This leaves us with 646,223 questionnaires over 20 years (1990–2010).

These questionnaires are handed out at the various border crossing ports, but not in a representative manner (either across ports, or across months of the year for a given port). Therefore, Statistics Canada has assigned weights to each questionnaire in order to address non-representative sampling and non-response. Applying these weights makes the data representative at the annual level for each port-factor-group (PFG).<sup>1</sup> However, we also want to exploit within-year variation in the exchange rate, and therefore require representative data on monthly travel. More importantly, we also require representative data at the level of each Census Division (CD) in order to examine the effect of the geographic distribution of residents on their propensity to travel. In order to construct data that are representative for each CD in each month, we construct our own weights.

Each questionnaire is associated with a particular CD and a port of entry into Canada. It also provides the month of travel and the length of the trip.<sup>2</sup> Therefore, each observation is CD-port-month-trip length combination. For notational clarity, we suppress subscripts for month and trip length. Define  $r_{cp}$  as the number of respondents from census division c passing through port of entry p. Define  $r_c$  as total respondents (across all CDs) at port p:  $r_p = \sum_c r_{cp}$ . Let  $n_p$  be the true number of crossers at port p which we obtain on a monthly basis from Cansim Table 427-0002. To estimate crossings by census division,  $\hat{n}_c$ , we first allocate  $n_p$  across census divisions using shares of response counts:  $\hat{n}_{cp} = (r_{cp}/r_p)n_p$ . Alternatively, one can think of this as the weighted sum of questionnaire respondents,  $r_{cp}$ , where weights are given by  $n_p/r_p$ , the number of actual crossers per respondent at a given port-month. Summing over all p for a given c we obtain  $\hat{n}_c = \sum_p r_{cp} n_p/r_p$ .

The estimated crossing fraction is given by dividing  $\hat{n}_c$  by our estimate of cars at risk,  $N_c = \text{Pop}_{ct} \times \text{CPC}_c \times 30$ . Census division populations,  $\text{Pop}_{ct}$ , are available annually from Cansim Table 051-0034, provided by Statistics Canada. Car registration

<sup>&</sup>lt;sup>1</sup>A PFG is a combination of a port of entry, length of stay, and mode of travel. For example, the PFG defined as Blaine–1 night–automobile is the set of traveling parties that entered Canada at the Blaine, BC port, having claimed to have spent one night in the US.

 $<sup>^{2}</sup>$ We construct the length of trip from the reported dates of exit and entry. We assign the month of travel as the calendar month in which the vehicle entered Canada.

data used for generating  $CPC_c$  come from Statistics Canada publication 53-219-XIB ("Road Motor Vehicle Registrations 1998").

### B.2 Driving distances and times to the border

We calculate the distance from each Canadian Census Division (similar to a US county) to the nearest ports  $D_c$  using two methods. The primary method takes advantage of geographically detailed information at the level of Census Subdivisions (similar to US Census Tracts). The 250 CDs have an average of 20 subdivisions. We obtained Subdivision centroid information from the Standard Geographical Classification of 2001 and used Google's driving distance application to measure the road distance and time from each centroid to the nearest crossing port. We obtained two measures: the median and the average distances for each CD. These two metrics are very similar for the majority of CDs except for two CDs in Ontario where the average distance is heavily influenced by outlier (low population and high distance to the border) subdivisions. We therefore used medians in our estimations. The results using averages do not differ much in terms of exchange rate or distance elasticities but the province and income effects are influenced by the two outliers.

The secondary method of calculating distances (employed in columns (5) and (6) of Table 3) takes into account the fact that crossers from a given census division do not always use the same port. At the CD level, we know shares of crossers from each CD that cross at 102 different ports. We use the average shares of the top 5 ports over the 1990 to 2010 period to construct weighted average distance and time from the CD's geographic centroid. This measure generates several outliers in large CDs that have centroids that are far from the border but populations that are concentrated close to the border.

### **B.3** Prices, exchange rates, and incomes

Exchange rates obtained from Pacific Exchange Rate Service (fx.sauder.ubc.ca). The US Consumer Price Index is the US city average for all items and all urban consumers, not seasonally adjusted (Series ID CUUR0000SA0 from bls.gov/cpi# data). Canadian prices are from CANSIM Table 3260020, 2009 basket, all items. We choose July 1993 as the base period because in that month the nominal exchange rate was equal to the annual purchasing power parity rate provided by the OECD and thus the RER was approximately 1. Prices for regular unleaded gasoline at self service filling stations are obtained from CANSIM Table 3260009 for a major urban centre for each of the border provinces. We obtained median household income from the CHASS Canadian Census Analyser for the years 1991, 1996, 2001, and 2006. We linearly interpolated and extrapolated around July of each census year to obtain the monthly data from 1990 to 2010.

# C Additional Tables

Table 1 presents summary statistics on the CBSA data used in Section 2 of the paper. Each observation is a calendar month in a given province.

	Mean	SD	Median	Min	Max
Day Trips (1000 vehicles):					
US	114.7	211.4	42.7	1	1224.8
CA	173.7	213.2	100.8	2.9	1192.9
Overnight Trips (1000 vehicles):					
US	41.7	71.9	14.4	0.5	519.1
CA	42.8	51.6	18.3	1.1	346.4
Nominal ER $(CAD/USD)$	1.236	0.166	1.221	0.962	1.6
Real ER	1.007	0.127	0.99	0.814	1.333

Table 1: Summary Statistics: 1972–2010 (3276 province-months)

Table 2 presents summary statistics for the ITS data and the distance, gas price, and income data we have merged onto it. The first column presents variable means across all observations, while the second column does so only for the subset of observations (39088) in which there was at least one car trip across the border in the given month. Conditioning on positive trips, Census Divisions tend to be closer to the border, and more populated. The large standard deviation for gas prices is mainly driven by temporal variation, whereas there is substantial cross-CD variation in household incomes.

Table 2: Summary Statistics: 63000 Census Divisions-months

Variable	Mean	$Mean trips>0^a$	SD	Median	Min	Max
Driving Distance (km)	263.0	187.0	281.2	161.9	6.8	1877.1
Driving time (hrs)	3.7	2.6	3.9	2.2	0.2	26.7
Population $(1000)$	116.2	165.8	273.8	40.8	1.2	2667.9
Gasoline Price $(c/L)$	73.5	72.5	21.1	66.5	39.5	146.6
Median HH Income (\$1000)	42.8	44.1	11.3	41.2	15.2	157.7
Cross-border trips (cars):						
Same-day	4093	6597	20229	0	0	456542
Overnight	1319	2126	4146	80	0	90662

<sup>a</sup> 39088 CD-months with at least one car trip across the border.

Table 3 presents the reasons that travelers give for crossing the border. These figures were derived from the International Travel Survey.

In Table 4 we present a regression that is analogous to Table 1 in the paper. It employs country-level data, instead of breaking up the data by provinces. That is, an

Trip Duration:	Sa	meday	Ov	ernight
Residence of Travelers:	US	Canada	US	Canada
Business Affairs	7.5	7.4	7.6	7.5
Visit friends/relatives	15.2	8.8	22.8	22.2
Pleasure or personal trip	43.1	53.2	62.3	64.6
Commuting to work	2.3	6.0	-	-
Other	21.1	15.4	7.2	5.5
Not stated	10.8	9.2	0.1	0.2
Total Respondents ('000s)	304	445	226	264

Table 3: Reasons for Crossing the Border, 1990–2010 (in percent)

Source: Authors' calculations from the International Travel Survey

observation is a country-month instead of a province-month. The results in the two tables are similar.

Length of stay:	Daytrip		Over	night	Daytrip		Overnight	
Residence:	US	CA	US	CA	US	CA	US	CA
$\ln e$	$1.54^{a}$	$-1.60^{a}$	$0.44^{c}$	$-1.49^{a}$	$1.38^{b}$	$-1.92^{a}$	0.46	$-1.66^{a}$
(CAD/USD)	(0.21)	(0.42)	(0.26)	(0.25)	(0.61)	(0.38)	(0.35)	(0.35)
$\ln e \times [e > 1.09]$ (strong USD)					$\begin{array}{c} 0.63 \\ (0.80) \end{array}$	$0.87^b$ (0.38)	$\begin{array}{c} 0.45 \\ (0.37) \end{array}$	0.42 (0.44)
$\ln e \times [e < 0.90]$					$-0.80^{c}$	$-0.73^{b}$	$-1.07^{a}$	-0.27
(strong CAD)					(0.41)	(0.33)	(0.38)	(0.34)
$R^2$	0.81	0.86	0.93	0.93	0.83	0.88	0.94	0.93

Table 4: Nation-level regressions of log crossings

Newey-West standard errors in parentheses are robust to serial correlation out to 60 months. Significance indicated by  $^{c} p < 0.1$ ,  $^{b} p < 0.05$ ,  $^{a} p < 0.01$ . N=468

To establish the robustness of the stylized facts in Section 2 of the paper, we also estimate using year-on-year differences of equation 1. That is, we subtract from each variable the value it had twelve months before. This holds constant season and province effects and also removes time-varying factors that may not have been well captured by the trend variables:

$$\ln n_{it} - \ln n_{i,t-12} = \{12\eta_3 + 144\eta_4\} + \eta_1 [\ln e_t - \ln e_{t-12}] + \eta_2 [post911_t - post911_{t-12}] + 24\eta_4 t + \varepsilon_{it} - \varepsilon_{i,t-12}.$$
(17)

The 12-month differences transform the linear trend into the constant term and the quadratic trend to a linear trend. The results of estimating this equation using country-level data are presented in Table 5.

Length of stay:	Daytrip		Overnight		Daytrip		Overnight	
Residence:	US	CA	US	CA	US	CA	US	CA
$\ln e$	$0.55^{a}$	$-1.17^{a}$	$0.26^{c}$	$-1.01^{a}$	$0.75^{b}$	$-1.24^{a}$	$0.26^{b}$	$-1.10^{a}$
(CAD/USD)	(0.20)	(0.27)	(0.14)	(0.26)	(0.32)	(0.26)	(0.12)	(0.29)
$\ln e \times [e > 1.09]$ (strong USD)					$\begin{array}{c} 0.01 \\ (0.23) \end{array}$	$\begin{array}{c} 0.22\\ (0.29) \end{array}$	$0.24^b$ (0.11)	$\begin{array}{c} 0.25 \\ (0.31) \end{array}$
$\ln e \times [e < 0.90]$ (strong CAD)					$-0.41^c$ (0.21)	-0.01 (0.19)	$-0.17^b$ (0.07)	0.02 (0.22)
$R^2$	0.17	0.52	0.04	0.27	0.19	0.52	0.07	0.27

Table 5: Nation-level regressions using year-on-year differences

New ey-West standard errors in parentheses are robust to serial correlation out to 60 months. Significance indicated by  $^c$   $p<0.1,\ ^b$   $p<0.05,\ ^a$ p<0.01. N=456

Table 6 shows the effect of including economic indicators, namely national GDP and employment rates, in the regression of cross-border travel on the Real Exchange Rate. The regression is at the country-month level. Note that there are fewer observations in this table than in Table 4. This is because the earliest year for which we could obtain comparable US and Canadian employment data was 1976.

The results show that adding economic variables does not change the main result. US elasticities are somewhat lower, while Canadian elasticities are somewhat higher, when these variables are included.

In Table 7 we present results of the various robustness checks described in Section 4.2 of the paper, using data on daytrips. The first column reproduces the results of our preferred specification, which is in Column 3 of Table 7. We do not report the province fixed effects in this table. The second column adds a quadratic term for log distance. This term is not significant and does not contribute significantly to the fit of the model.

In column 3, we add an interaction between the distance and exchange rate variables. Once again, this term is not significant. In columns 4 and 5 we drop census divisions with implausibly long daytrips. Column 4 drops the 14 CDs where the driving time to the border is 12 hours or more, Column 5 drops the 95 CDs for which the driving time is at least 3 hours. In both cases the estimated coefficients remain stable.

Finally, in Column 6 we drop the 14 census divisions where at least 10% of crossborder travelers identify as commuters. These are generally CDs that are very close to the border, and located near large US cities. Once again, the results are robust to dropping these observations.

In Table 8, we present the results of regressing mean and median expenditures reported by Canadians traveling in the US on the RER. Expenditures are expressed

Length of stay:	Day	vtrip	Over	night	Day	trip	Over	night
Residence:	US	CA	US	CA	US	CA	US	CA
$\ln e$	$1.43^{a}$	$-1.71^{a}$	$0.33^{c}$	$-1.51^{a}$	$1.04^{a}$	$-2.14^{a}$	$0.12^{c}$	$-1.75^{a}$
(CAD/USD)	(0.15)	(0.33)	(0.18)	(0.26)	(0.20)	(0.24)	(0.07)	(0.22)
$\ln$ US GDP					-2.05	$-1.84^{c}$	$1.83^{a}$	$-2.40^{b}$
					(2.58)	(1.07)	(0.42)	(1.18)
$\ln CA GDP$					$-1.77^{a}$	$-2.16^{a}$	$-1.47^{a}$	$-1.46^{a}$
					(0.52)	(0.25)	(0.23)	(0.31)
ln US employment					2.40	0.27	$-2.87^{a}$	0.58
					(2.07)	(0.84)	(0.77)	(1.07)
ln CA employment					2.64	0.49	$1.81^{a}$	0.12
1 0					(2.15)	(0.66)	(0.48)	(0.77)
N	408	408	408	408	408	408	408	408
$R^2$	0.80	0.89	0.95	0.93	0.86	0.94	0.96	0.94
RMSE	0.15	0.11	0.14	0.12	0.13	0.08	0.12	0.11

Table 6: Nation-level regressions of log crossings

New ey-West standard errors in parentheses are robust to serial correlation out to 60 months. Significance indicated by  $^c$   $p<0.1,\ ^b$   $p<0.05,\ ^a$ p<0.01.

	(1)	(2)	(3)	(4)	(5)	(6)
$\theta_0$ : constant	$4.42^{a}$	$4.34^{a}$	$4.39^{a}$	$4.50^{a}$	$5.38^{a}$	$5.32^{a}$
	(1.52)	(1.53)	(1.53)	(1.55)	(1.79)	(1.51)
$\theta_1$ : ln $e_t$ [RER]	$-0.65^{a}$	$-0.65^{a}$	-0.33	$-0.65^{a}$	$-0.66^{a}$	$-0.69^{a}$
	(0.13)	(0.13)	(0.39)	(0.13)	(0.14)	(0.13)
$\theta_2$ : $(\ln e_t)^2$	$0.82^{b}$	$0.85^{a}$	$0.79^{b}$	$0.81^{b}$	$0.85^{b}$	$0.82^{b}$
	(0.33)	(0.33)	(0.34)	(0.33)	(0.36)	(0.34)
$\theta_2$ : ln $D_2$ [distance]	$-0.52^{a}$	-0.20	$-0.51^{a}$	$-0.52^{a}$	$-0.52^{a}$	$-0.53^{a}$
- ] [ []	(0.04)	(0.34)	(0.04)	(0.04)	(0.04)	(0.04)
$(\ln D_c)^2$		-0.04				
(		(0.04)				
$(\ln e_t) * (\ln D_c)$			-0.08			
$(\dots \circ_l) \land (\dots \circ_l)$			(0.09)			
$\ln P(q)_{ct}$ [gas price]	-0.07	-0.06	-0.07	-0.07	-0.07	$-0.08^{c}$
	(0.05)	(0.05)	(0.05)	(0.05)	(0.05)	(0.05)
$\ln W_{ct}$ [income]	$-0.42^{a}$	$-0.46^{a}$	$-0.41^{a}$	$-0.42^{a}$	$-0.50^{a}$	$-0.49^{a}$
	(0.14)	(0.14)	(0.14)	(0.14)	(0.17)	(0.14)
Post-911	$-0.14^{a}$	$-0.14^{a}$	$-0.14^{a}$	$-0.14^{a}$	$-0.14^{a}$	$-0.15^{a}$
	(0.03)	(0.03)	(0.03)	(0.03)	(0.03)	(0.03)
N	63000	63000	63000	59472	39060	59472
$R^2$	0.53	0.56	0.53	0.53	0.53	0.54
AIC	1778.11	1777.81	1779.95	1765.00	1660.78	1681.54

Table 7: Fractional Probit Regressions: Robustness Checks for Daytrips  $(x_{ct})$ 

Standard errors clustered by census-division. Regressions include month and province fixed-effects.  $^{c}$  p<0.1,  $^{b}$  p<0.05,  $^{a}$  p<0.01.

in constant 2002 dollars. The first two columns report results for daytrips, and the next two for overnight trips.

	Day	trips	Overnight trips		
	median	average	median	average	
$\ln e$	$-0.30^{a}$	$-0.95^{a}$	-0.14	0.17	
(RER)	(0.10)	(0.28)	(0.14)	(0.10)	
Constant	$3.28^{a}$	$3.86^{a}$	$6.47^{a}$	$7.08^{a}$	
	(0.04)	(0.08)	(0.05)	(0.04)	
# obs.	252	252	252	252	
$R^2$	0.63	0.53	0.83	0.94	

Table 8: Regressions of Log Median and Average Real Expenditures

SEs clustered by year-month. Month dummies, trend and trend squared included but not reported.  $^a$  p<0.01.

The estimated elasticities are negative and significant for daytrips, but statistically insignificant for overnight trips. The results show that Canadian daytrippers increase their spending in the US when the CAD appreciates, while overnight travelers do not. The results are robust to using both median as well as mean expenditures. This is corroborating evidence for the hypothesis that consumers making day trips expand the bundle of goods they purchase in the US, consistent with an explicit shopping motive, but that overnight travelers do not exhibit such behavior.

In Table 9, we present regressions showing the effect of weather on same day and overnight travel. The first specification is our preferred (column 3) specification in Table 5 in the paper. It includes all the month dummies but we only report July since it illustrates the main seasonal pattern. The second column replaces month dummies with data on temperature, snowfall, and precipitation. The positive impact of temperature almost completely explains the seasonal pattern. The mean temperature in July is  $20^{\circ}$ C,  $28^{\circ}$ C higher than the mean temperature in January. The coefficient on temperature implies a 0.14 difference for July, about what the month dummy in the first specification indicated. Weather has no significant effect on daytrips in the third regression that includes month fixed-effects. This means that deviations from average monthly weather do not affect same-day travel. The story is somewhat different for trips that last one or more nights. There we see stronger weather effects (but the seasonal pattern was also stronger in the dummies so that is not surprising). Deviations from weather means do affect overnight trips, especially snowfall.

Table 10 shows that different distributional assumptions do not affect the calculation of travel costs.

Tables 11 and 12 decompose the welfare changes generated a 10% appreciation of the Canadian dollar and increasing wait times at the border. The total welfare effects of the counterfactuals are explained and reported in Table 8 in the paper.

		Daytrip			Overnight	t.
July vs January	$0.159^{a}$		$0.133^{a}$	$0.337^{a}$		$0.420^{a}$
	(0.021)		(0.039)	(0.018)		(0.038)
Temp (deg C, mo. mn)		$0.005^{a}$	0.001		$0.008^{a}$	$-0.005^{a}$
		(0.001)	(0.002)		(0.001)	(0.001)
Snow (m, mo. accum.)		-0.018	0.000		$-0.073^{a}$	$-0.190^{a}$
		(0.032)	(0.028)		(0.019)	(0.030)
Precip. (cm, mo. accum.)		-0.001	-0.001		$-0.002^{a}$	0.001
		(0.001)	(0.001)		(0.001)	(0.001)
Month effects	yes	no	yes	yes	no	yes
N	63000	62902	62902	63000	62902	62902
$R^2$	0.535	0.532	0.535	0.078	0.068	0.078
log-like	-865.1	-864.878	-864.439	-294.3	-295.7	-294.0
Standard errors in parentheses $^{c} p < 0.1$ , $^{b} p < 0.05$ , $^{a} p < 0.01$						

Table 9: Crossing fraction regressions including weather

Table 10: Travel cost estimates

Distribution	$d\ln e/d\ln D$	US \$/mile		$d\ln e/d\ln T$	US \$/hour	
		median	average		median	average
$\zeta(i) \sim \text{Normal}$	-0.611	0.87	1.66	-1.023	29.69	68.34
$\zeta(i) \sim \text{Logistic}$	-0.618	0.88	1.68	-1.124	32.63	75.10
$\zeta(i) \sim \text{Gumbel}$	-0.597	0.85	1.63	-0.946	27.47	63.23

Year:		2002	2010		
	$\% \Delta$ Trips $(n_c)$	$\% \Delta \text{ Gains } (G_c/n_c)$	$\% \Delta$ Trips	$\%~\Delta$ Gains	
Canada	8.02	0.68	25.67	2.22	
New Brunswick	6.33	0.80	19.92	2.59	
Quebec	10.00	0.67	32.12	2.18	
Ontario	7.94	0.69	25.47	2.24	
Toronto $(140 \text{ km})$	10.78	0.67	34.35	2.19	
Hamilton $(75 \text{ km})$	9.79	0.71	31.30	2.32	
Niagara $(24 \text{ km})$	8.08	0.81	25.21	2.62	
Manitoba	9.76	0.68	31.35	2.20	
Saskatchewan	10.47	0.61	34.02	1.98	
Alberta	11.41	0.58	37.81	1.86	
British Columbia	8.31	0.76	25.88	2.47	

Table 11: Impact of a 10% Canadian dollar appreciation on same-day travel

Table 12: Impact of a doubling of border wait times on same day trips

Year:	2002		2010		
	$\% \Delta$ Trips	$\% \Delta$ Gains	$\% \Delta$ Trips	$\% \; \Delta \; \mathrm{Gains}$	
Canada	-57.08	-4.51	-54.60	-4.61	
New Brunswick	-52.29	-5.05	-49.10	-5.16	
Quebec	-55.77	-4.44	-54.04	-4.58	
Ontario	-60.37	-4.92	-57.33	-5.01	
Toronto $(140 \text{ km})$	-44.74	-4.00	-42.84	-4.17	
Hamilton $(75 \text{ km})$	-53.72	-6.01	-52.32	-6.17	
Niagara $(24 \text{ km})$	-64.16	-9.49	-62.53	-9.74	
Manitoba	-53.42	-3.89	-51.78	-4.03	
Saskatchewan	-53.31	-2.20	-51.48	-2.22	
Alberta	-50.75	-1.63	-49.23	-1.66	
British Columbia	-55.38	-5.96	-53.48	-6.22	

# D Additional Figures



Figure D.1: Census Divisions in Southeastern Ontario



Figure D.2: Accumulated Population and Distance to the Border: Canada (solid) and US (dashed) 14