

MATH 110-003, QUIZ 3

October 20, 2016

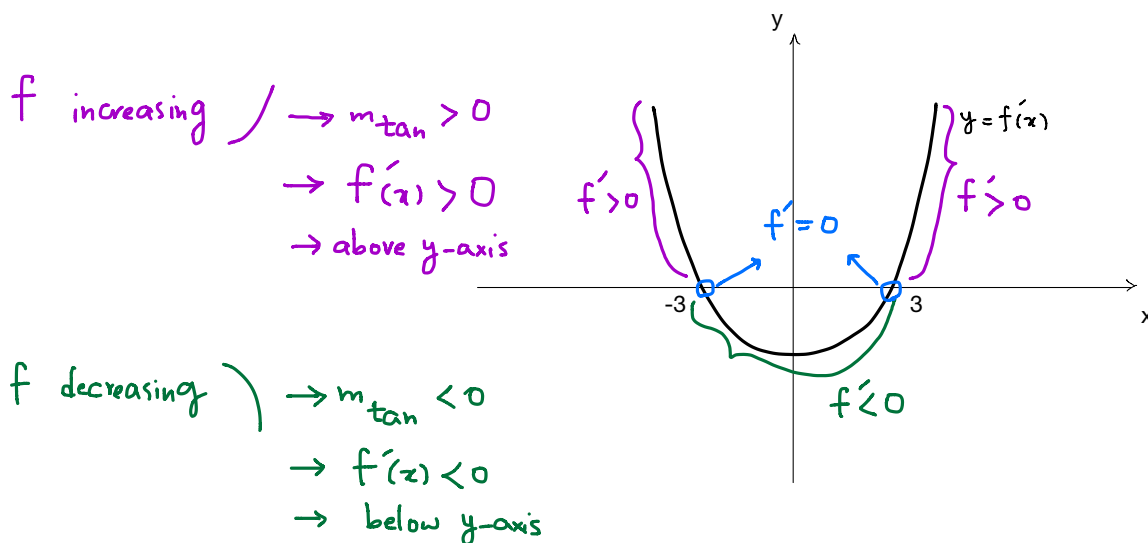
Time: 15 minutes

Show all your work. No calculators, no books/notes are allowed.

Name (please print): _____

Student number: _____

1. The graph of the derivative f' is shown below. Answer the following questions about the function f .



a) For what values of x is f increasing?

$$x < -3 \text{ and } x > 3$$

$$(-\infty, -3) \text{ and } (3, +\infty) \leftarrow \text{Interval notation}$$

b) For what values of x is f decreasing?

$$-3 < x < 3 \text{ or } (-3, 3)$$

c) For what values of x does f have a horizontal tangent line?

$$x = -3 \text{ and } x = 3$$

(Hint: The answer to each part can be an interval.)

2. Let f be the function $f(x) = x^3 - 3x$

(a) Find all points on the graph at which the tangent line to f is parallel to the line $y = 9x + 4$. (Find both x and y coordinates of the points.)

(b) Write the equation of the tangent line to f at the point with positive x -coordinate from part (a).

(a)

tangent line parallel to $y = 9x + 4$

$$\Rightarrow m_{\text{tan}} = 9 \quad \leftarrow \text{slope}$$

On the other hand

$$m_{\text{tan}} = f'(x)$$

$$f'(x) = 9$$

Use power rule, find $f'(x)$ and solve the equation.

$$f(x) = x^3 - 3x \Rightarrow f'(x) = 3x^2 - 3$$

$$f'(x) = 9 \Rightarrow 3x^2 - 3 = 9$$

$$\Rightarrow 3x^2 = 12$$

$$\Rightarrow x^2 = 4$$

$$\Rightarrow x = 2, \quad x = -2$$

$$\text{plug into } f \Rightarrow y = 2^3 - 3(2), \quad y = (-2)^3 - 3(-2)$$

$$= 2, \quad = -2$$

$$(2, 2), \quad (-2, -2)$$

(b) $(2, 2)$ is the point with positive x -coordinate

$$(m_{\text{tan}} \text{ at } x=2) = f'(2) = 3(2)^2 - 3 = 9$$

$$y - y_1 = m_{\text{tan}}(x - x_1)$$

$$y - 2 = 9(x - 2) \rightarrow y = 9x - 16$$

You can skip this part and just use the fact that: tangent line is parallel to $y = 9x + 4$ so $m_{\text{tan}} = 9$