

MATH 110-001, QUIZ 3

February 16, 2018

Time: 10 minutes

Show all your work. No calculators, no books/notes are allowed.

Name (please print): _____

Student number: _____

1. Consider a function f whose derivative is given by

$$f'(x) = \frac{x^2}{x-1},$$

complete the following sign chart to determine the concavity of f and its inflection points. Also, write down the intervals where f is concave up and concave down.

We need to find $f''(x)$ by applying quotient rule.

$$f''(x) = \frac{2x(x-1) - x^2}{(x-1)^2} = \frac{x^2 - 2x}{(x-1)^2} \quad \begin{array}{l} \nearrow f''(x) = 0 \Rightarrow x(x-2) = 0 \quad \begin{array}{l} \nearrow x = 0 \\ \searrow x = 2 \end{array} \\ \searrow f''(x) \text{ NOT defined} \Rightarrow (x-1)^2 = 0 \Rightarrow x = 1 \end{array}$$

x	$-\infty$	\uparrow	$x = -1$	\uparrow	$x = \frac{1}{2}$	\uparrow	$x = \frac{3}{2}$	\uparrow	test $x = 3$	$+\infty$
$f''(x)$	$+$		0		$-$		∞		$-$	$+$
$f(x)$	\cup		INF point		\cap		\cap		INF point	\cup

$$f'' = \frac{\text{always } +}{+}$$

$$f''(3) = \frac{9-6}{+} > 0$$

$$f''(\frac{3}{2}) = \frac{\frac{9}{4} - \frac{6}{2}}{+} < 0$$

$$f''(\frac{1}{2}) = \frac{\frac{1}{4} - 1}{+} < 0$$

$$f''(-1) = \frac{1-2(-1)}{+} > 0$$

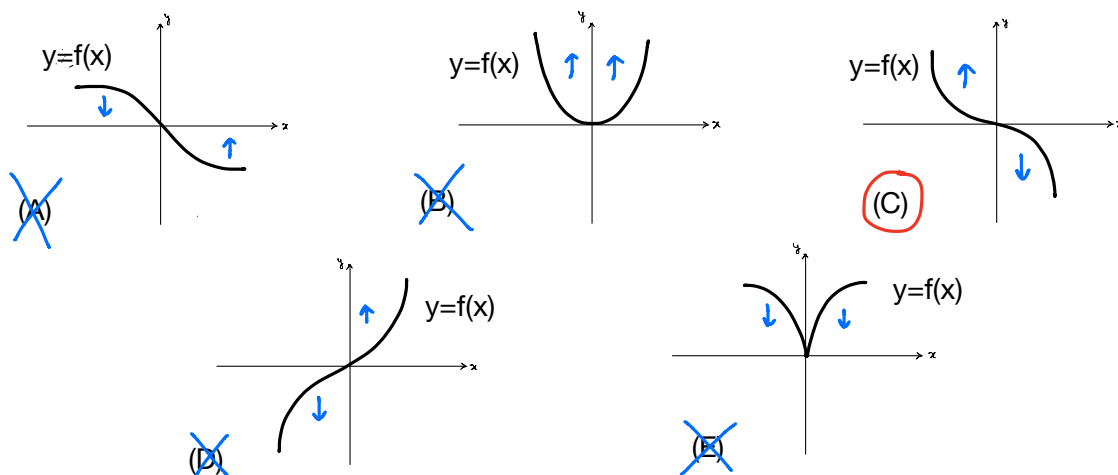
Interval(s) where f is concave **up**: $(-\infty, 0)$, $(2, \infty)$

Interval(s) where f is concave **down**: $(0, 1)$, $(1, 2)$

Inflection point(s) of f : $x = 0, 2$

2. Choose the graph of the function f for which

- $f''(x) > 0$ in $(-\infty, 0)$ \longrightarrow Concave up to the left of $x=0$
- and
- $f''(x) < 0$ in $(0, \infty)$ \longrightarrow Concave down to the right of $x=0$



3. **(Bonus)** Choose three of the following resources that you will most likely use to prepare for the midterm:

- | | |
|----------------------------|-----------------------|
| Textbook | <input type="radio"/> |
| Lecture notes | <input type="radio"/> |
| WebWork problems | <input type="radio"/> |
| Quiz/HW problems | <input type="radio"/> |
| Workshop problems | <input type="radio"/> |
| Past Exams (MER wiki page) | <input type="radio"/> |