

### QUIZ 3

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First name:

Last name:

Student number:

Recitation section:

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1. Find the antiderivative (indefinite integral)  $\int \sin^4(x) \cos^3(x) dx$ .

$$\begin{aligned}\int \sin^4(x) \cos^3(x) dx &= \int \sin^4(x) \cos^2(x) \cos(x) dx \\ &= \int \sin^4(x) (1 - \sin^2(x)) \cos(x) dx \\ \text{Let } u = \sin(x) &= \int u^4 (1 - u^2) du \\ du = \cos(x) dx & \\ &= \frac{u^5}{5} - \frac{u^7}{7} + C \\ &= \frac{\sin^5(x)}{5} - \frac{\sin^7(x)}{7} + C\end{aligned}$$

Note! Whenever you have a trig integral like this, you need to make sure you have one  $\sin(x)$  or  $\cos(x)$  leftover for your  $du$ .

2. Evaluate the integral  $\int_0^1 t e^{-2t} dt$ .

$$\begin{aligned}\int_0^1 t e^{-2t} dt & \text{ Use integration by parts with } u=t \Rightarrow du=dt \\ & dv=e^{-2t} dt \Rightarrow v=\frac{-1}{2}e^{-2t} \\ &= u \cdot v \Big|_0^1 - \int_0^1 v du \\ &= \frac{-t e^{-2t}}{2} \Big|_0^1 - \int_0^1 \frac{-1}{2} e^{-2t} dt \\ &= \left( \frac{-e^{-2}}{2} - 0 \right) + \frac{1}{2} \left( \frac{-1}{2} e^{-2t} \Big|_0^1 \right) \\ &= \frac{-1}{2e^2} + \frac{1}{2} \left( \frac{-1}{2} e^{-2} + \frac{1}{2} e^0 \right) \\ &= \frac{-1}{2e^2} - \frac{1}{4e^2} + \frac{1}{4} \\ &= \frac{-3}{4e^2} + \frac{1}{4}\end{aligned}$$